

A Parallel Approach to Syllabification

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Abstract. In this paper we propose a parallel manner of syllabification introducing some parallel extensions of insertion grammars. We use this grammars in an application to Romanian language syllabification.

1 Introduction

In formal language theory, most of the generative mechanisms investigated are based on the *rewriting* operation. Several other classes of mechanisms, whose main ingredient is the *adjoining* operation, were introduced along the time. The most important of them are *the contextual grammars* (Marcus, 1969), *the tree adjoining grammars* (TAG) (Joshi et al., 1975) and *the insertion grammars* (Galiukschov, 1981), all three of them introduced with linguistic motivations. Contextual grammars were introduced by Marcus (1969) and have their origin in the attempt to bridge the gap between the structuralism and generativism. The insertion grammars (or semi-contextual grammars) are somewhat intermediate between Chomsky context-sensitive grammars (where the non-terminal are rewritten according to specified contexts) and contextual grammars (where contexts are adjoined to specified strings associated with contexts).

In this paper we introduce some parallel extensions of insertion grammars and we use them to propose a parallel manner of word syllabification. Up to now, from our knowledge, most of the formal models of syllabification were treated in a sequential manner (Vennemann (1978), Koskenniemi (1983), Bird and Ellison (1994), Kaplan and Kay (1994), Muller (2002), Dinu (2003)).

This paper is structured as follows: in Section 2 we present *the insertion grammars* and introduce two new variants of them: *parallel insertion grammars* and *maximum parallel insertion grammars*. The syllabification of words, the definition of syllable and an application (Romanian words syllabification) of this approach of syllabification is given in Section 3.

2 Parallel Extensions of Insertion Grammars

For elementary notions of formal language theory, such as *alphabet*, *concatenation*, *language*, *free monoid*, *lengths of words*, etc. we refer to (Păun, 1997).

The basic operation in insertion grammars is the adjoining of strings, as in contextual grammars, not rewriting, as in Chomsky grammars, but the operation is controlled by a context, as in context-sensitive grammars.

Definition 1 (Păun, 1997). *An insertion grammar is a triple $G = (V, A, P)$, where V is an alphabet, A is a finite language over V , and P is a finite set of triples of strings over V .*

The elements in A are called axioms and those in P are called insertion rules.

The meaning of a triple $(u, x, v) \in P$ is: x can be inserted in the context (u, v) . Specifically, for $w, z \in V^$ we write $w \Rightarrow z$ if $w = w_1 u v w_2$, $z = w_1 u x v w_2$, for $(u, x, v) \in P$ and $w_1, w_2 \in V^*$.*

The language generated by G is defined by: $L(G) = \{z \in V^* \mid w \xRightarrow{*} z, \text{ for } w \in A\}$.

Here we introduce two parallel extensions of insertion grammars.

Definition 2. *Let $G = (V, A, P)$ be an insertion grammar. We define the parallel derivation denoted \Rightarrow_p , by:*

$w \Rightarrow_p z$ iff $w = w_1 w_2 \dots w_r$, for some $r \geq 2$, $z = w_1 x_1 w_2 x_2 w_3 \dots x_{r-1} w_r$ and, for all $1 \leq i \leq r - 1$, there is $(u_i, x_i, v_i) \in P$ and $\alpha_i, \beta_i \in V^$ such that $w_i x_i w_{i+1} = \alpha_i u_i x_i v_i \beta_i$ and $w_i = \alpha_i u_i$, $w_{i+1} = v_i \beta_i$.*

Remark 1. For usual derivation \Rightarrow we use one selector-pair, with no restriction; in parallel derivations the whole string is decomposed into selectors.

Definition 3. *For an insertion grammar $G = (V, A, P)$ we define the parallel derivation with maximum use of insertions (in short, we say maximum parallel derivation), denoted \Rightarrow_{pM} , by:*

$w \Rightarrow_{pM} z$ iff $w = w_1 w_2 \dots w_s$, $z = w_1 x_1 w_2 x_2 w_3 \dots x_{s-1} w_s$, $w \Rightarrow_p z$ and there is no $n > s$ such that $w = w'_1 w'_2 \dots w'_n$, $z' = w'_1 x'_1 w'_2 x'_2 w'_3 \dots x'_{n-1} w'_n$, $w \Rightarrow_p z'$.

Remark 2. The main difference between parallel derivation (\Rightarrow_p) and maximum parallel derivation (\Rightarrow_{pM}) with respect to an insertion grammar is that in the former we can insert any number of strings in a derivation step and in the later we insert the maximum possible number of strings in a derivation step.

For $\alpha \in \{p, pM\}$, we denote by $L_\alpha(G)$ the language generated by the grammar G in the mode α :

$$L_\alpha(G) = \{z \in V^* \mid w \xRightarrow{*}_\alpha z, \text{ for some } w \in A\}.$$

The family of such languages is denoted by INS_α , $\alpha \in \{p, pM\}$.

We give here (without proofs) some results regarding the relations between INS_{pM} and Chomsky hierarchy.