

# ATLAS results on exotic hadrons

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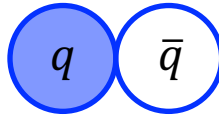


ICHEP 2024

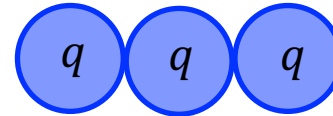
July 18-24, Prague, Czech

# Introduction – exotic hadrons

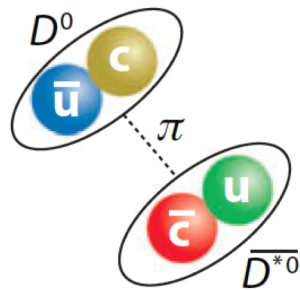
Traditional quark models:



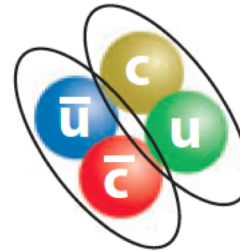
Meson



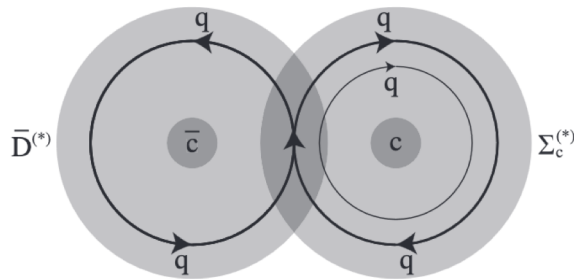
Baryon



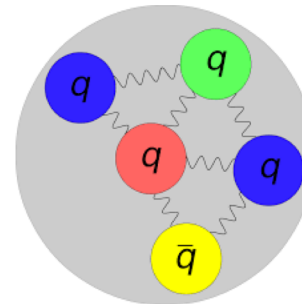
$D^0$ - $\bar{D}^{*0}$  "molecule"



Diquark-diantiquark



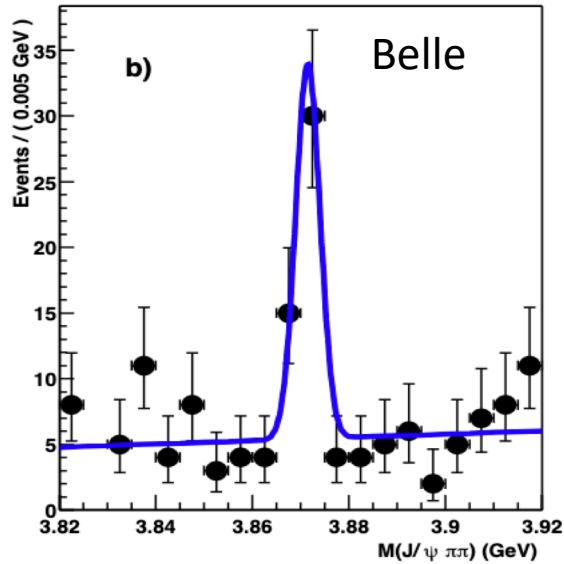
Meson + baryon "molecule"



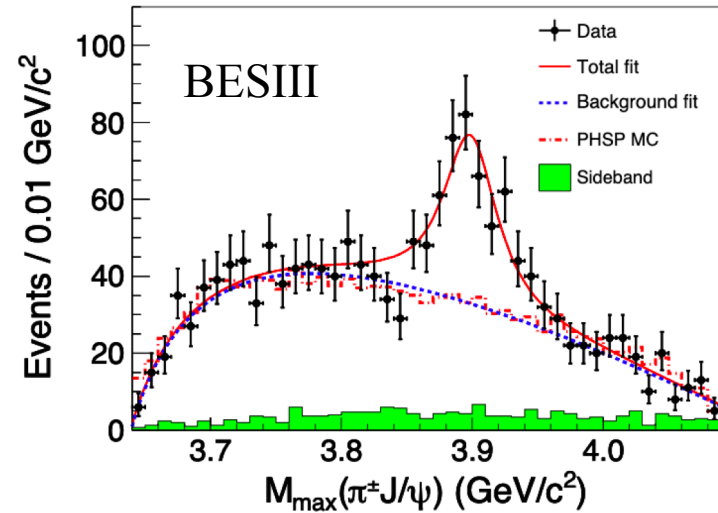
Pentaquark

# Hidden charm tetraquark

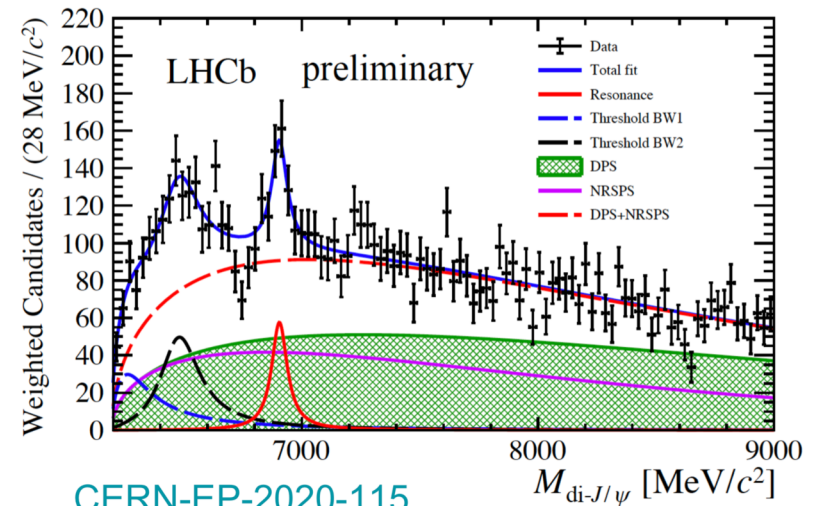
[ Phys. Rev. Lett 91 (2003) 262001 ]



[ Phys.Rev.Lett. 110 (2013) 252001 ]

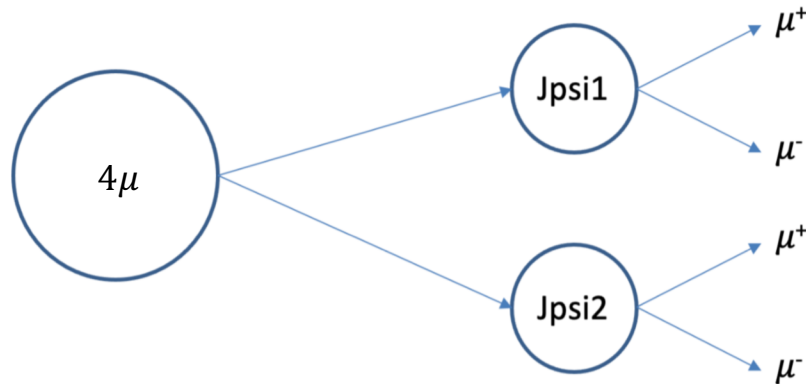


- X(3872) at Belle, Y(4260) at BABAR, Z<sub>c</sub><sup>+</sup>(3900) at BESIII, and later a number of XYZ states ...
- Charmed Tetraquark (TQ) state is often proposed for these LS
- Potential 4-charm TQ from LHCb

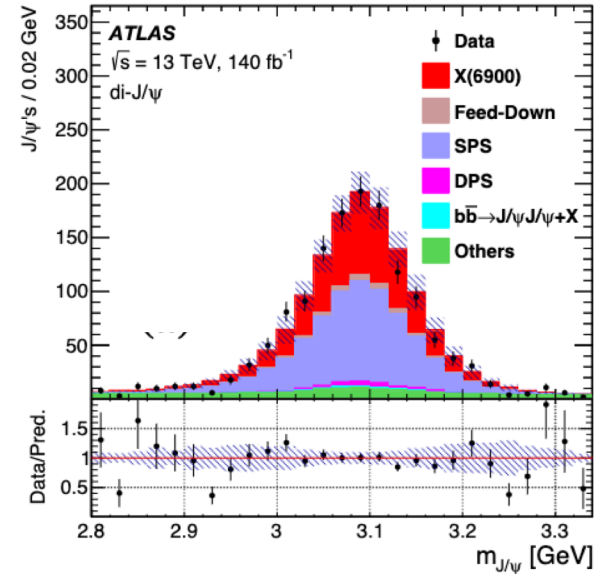


[CERN-EP-2020-115](#)

# Reconstruction of $4\mu$ vertex at ATLAS



[ Phys. Rev. Lett. 131 (2023) 151902 ]



- We first find vertices of  $J/\psi$  candidates and geometrically fit the 4 tracks of a  $J/\psi$  pair to a common vertex. We revertex two  $J/\psi$  tracks with a mass constraint, improving the  $4\mu$  mass resolution from  $\sim 95 \text{ MeV}$  to  $\sim 20 \text{ MeV}$
- Use sum of  $\chi^2/N$  of two charmonia and  $4\mu$  vertices to select the best  $4\mu$  candidate per event

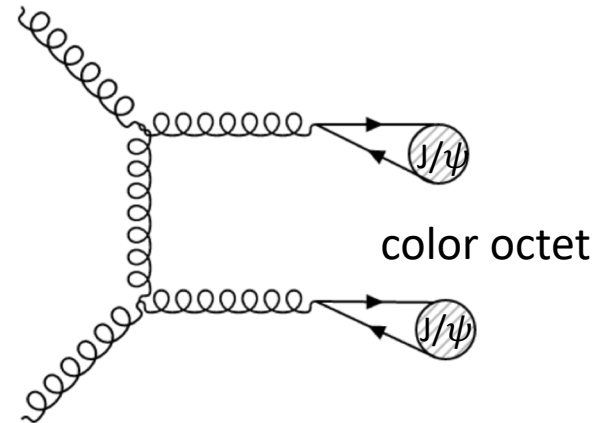
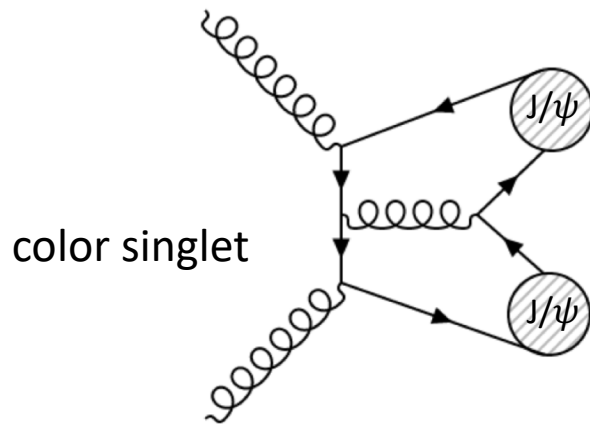
# Signal and Backgrounds

- Signal process
  - Signal samples for process:  $pp \rightarrow X \rightarrow \text{di-}J/\psi \rightarrow 4\mu$ 
    - TQ mass = 6.9 GeV, width = 0.1 GeV, spin = 0 with JHU
- Background processes:
  - Prompt di- $J/\psi$  background: Single Parton Scattering (SPS), Double Parton Scattering (DPS) with Pythia8
  - Non prompt di- $J/\psi$  background:  $b\bar{b} \rightarrow J/\psi J/\psi$  with Pythia8
  - Single  $J/\psi$  background
    - Prompt or nonprompt  $J/\psi$ , plus fake muons from the primary vertex
  - Non-peaking background containing no real  $J/\psi$  candidates

Single  $J/\psi$  background and non-peaking background are collectively called “others”, and are estimated from data by reversing one muon’s ID

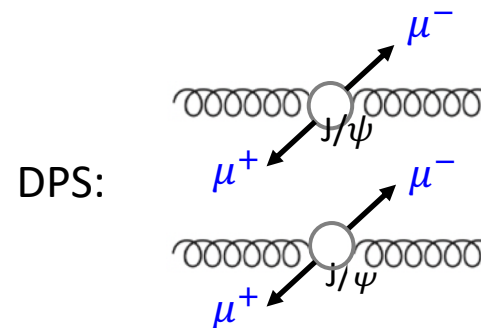
# SPS and DPS backgrounds

- Both color singlet and color octet processes are included for di-charmonium SPS, dominated by gluon-gluon interactions. As a result, the two  $J/\psi$ 's from SPS are highly correlated



- DPS populates the relatively low- $p_T$  region, and becomes more important with larger collider energy, as the parton density increases at small  $x$
- If neglecting correlations between partons (effective cross section approximation):

$$\sigma_{\text{eff}} = \frac{1}{2} \frac{\sigma_{J/\psi}^2}{\sigma_{\text{DPS}}^{J/\psi, J/\psi}}$$

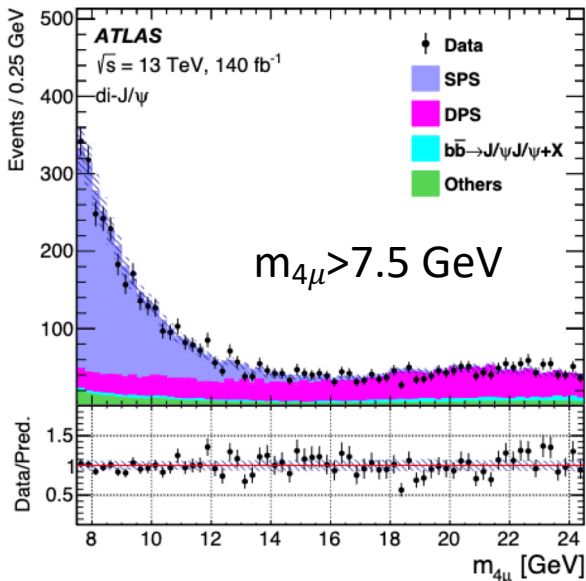
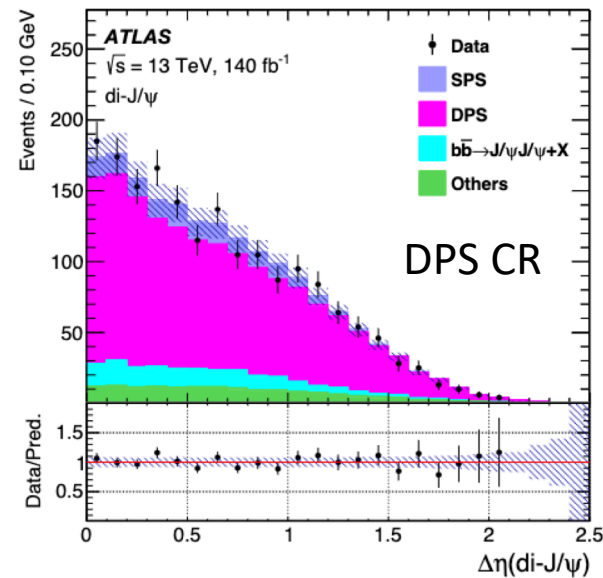
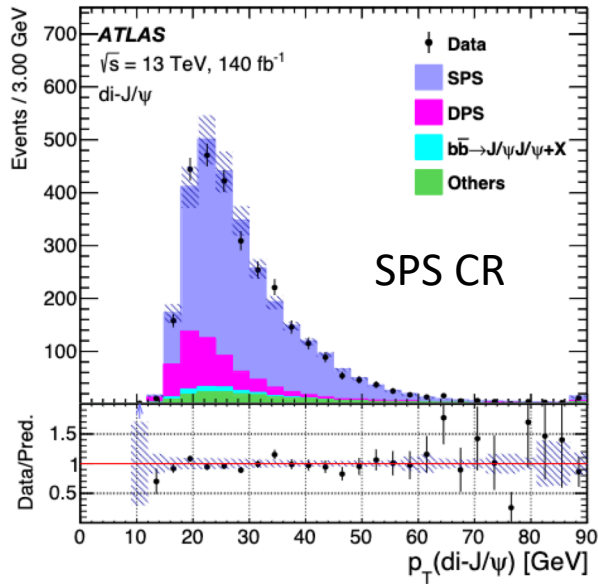


# Event selection

Signal region	Control region	Non-prompt region
Di-muon or tri-muon triggers, oppositely charged muons from each charmonium, <i>loose</i> muons, $p_T^{1,2,3,4} > 4, 4, 3, 3$ GeV and $ \eta_{1,2,3,4}  < 2.5$ for the four muons, $m_{J/\psi} \in [2.94, 3.25]$ GeV, or $m_{\psi(2S)} \in [3.56, 3.80]$ GeV, Loose vertex requirements $\chi_{4\mu}^2/N < 40$ ( $N = 5$ ) and $\chi_{\text{di-}\mu}^2/N < 100$ ( $N = 2$ ),		
Vertex $\chi_{4\mu}^2/N < 3$ , $L_{xy}^{4\mu} < 0.2$ mm, $ L_{xy}^{\text{di-}\mu}  < 0.3$ mm, $m_{4\mu} < 11$ GeV,		Vertex $\chi_{4\mu}^2/N > 6$ ,
$\Delta R < 0.25$ between charmonia	$\Delta R \geq 0.25$ between charmonia	or $ L_{xy}^{\text{di-}\mu}  > 0.4$ mm

- Signal region cuts:
  - di- $\mu$  or tri- $\mu$  triggers per year for maximum efficiency
  - 4 muons with minimum  $p_T$  of 3 GeV within acceptance
  - Vertex  $\chi^2/N$  cut,  $J/\psi$  mass window cuts
  - $L_{xy}$  (distance between  $J/\psi$  and PV vertices) cut
  - $\Delta R < 0.25$  of two  $J/\psi$ 's
- SPS and DPS are estimated by MC, and are kinematically corrected by SPS and DPS enriched  $4\mu$  mass sidebands (SPS and DPS CRs)
- Non-prompt  $J/\psi$  background is estimated with data by reversing the  $L_{xy}$  or  $\chi^2/N$  cut

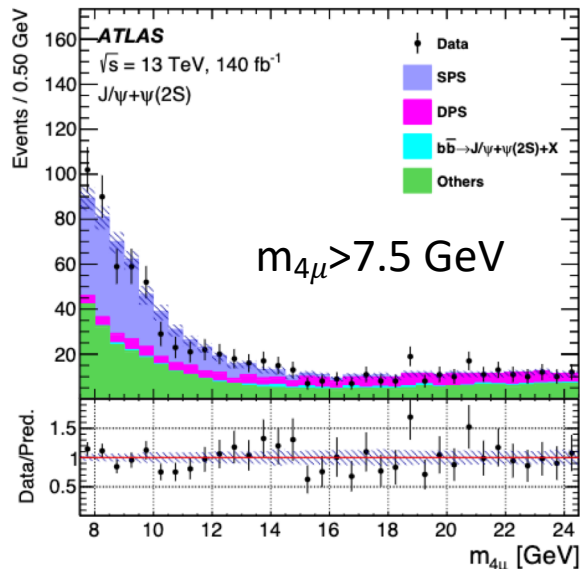
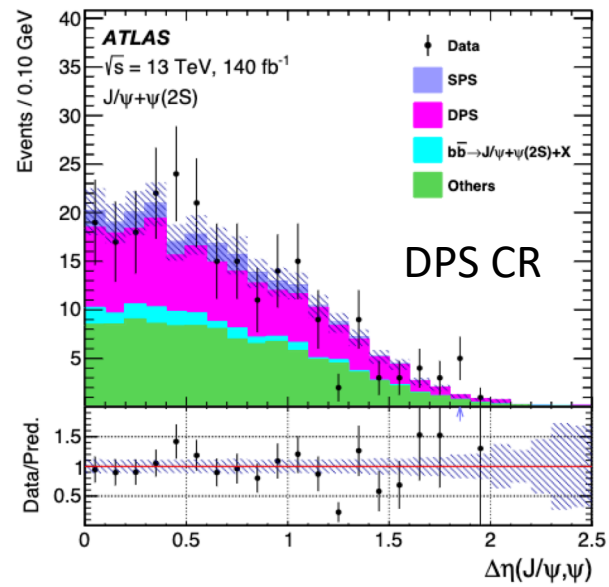
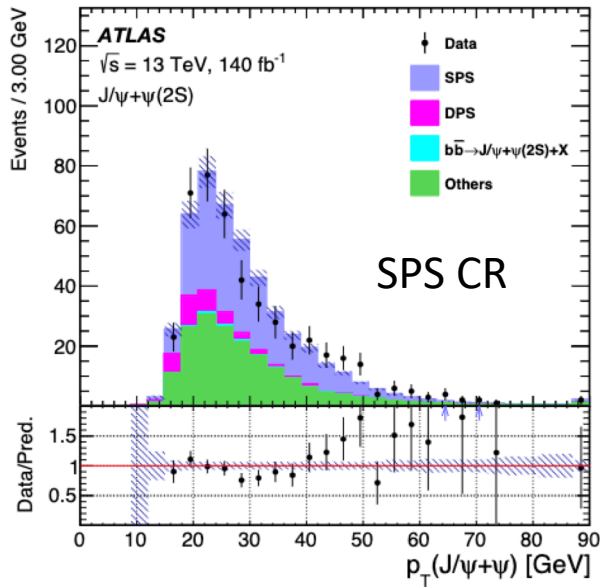
# SPS and DPS CRs in di- $J/\psi$ channel



- Discrepancies in some kinematics distributions are resolved by event reweighting in the SPS and DPS CRs without  $\Delta R$  cut
  - ✓ SPS CR:  $7.5 \text{ GeV} < m_{4\mu} < 12.0 \text{ GeV}$
  - ✓ DPS CR:  $14.0 \text{ GeV} < m_{4\mu} < 24.5 \text{ GeV}$
- After reweighting, other kinematic distributions are also improved

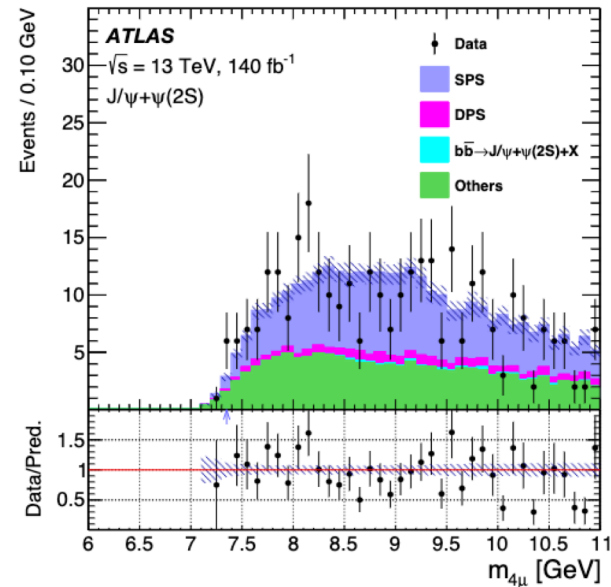
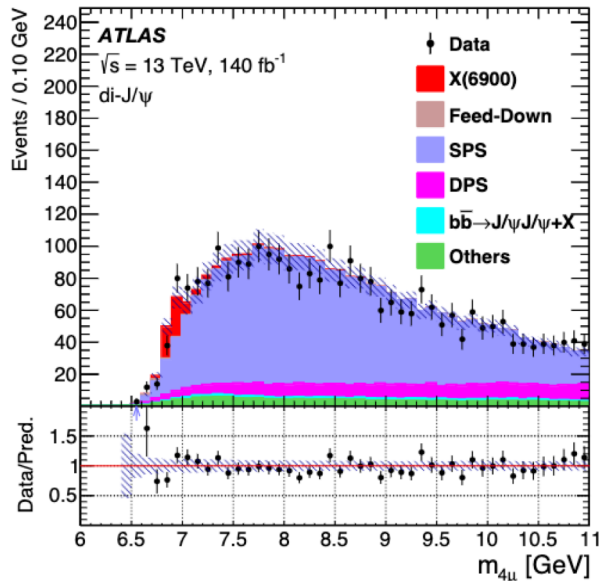


# SPS and DPS CRs in $J/\psi+\psi(2S)$ channel



- Larger “others” background due to smaller signal/background ratio for  $\psi(2S)$
- SPS and DPS are also corrected through reweighting method ( after “others” corrections in its dedicated CR –  $J/\psi$  mass sidebands)

# Control region ( $\Delta R > 0.25$ )



- The control region has the same cuts as the signal region, but with  $\Delta R > 0.25$  between two  $J/\psi$ 's. It serves two purposes
  - ✓ Correct and validate the SPS  $4\mu$  mass shape. Pythia8 *pT0timesMPI* parameter is first tuned to data in SPS CR in  $m_{4\mu} > 7.5$  GeV, and validated in the control region with  $m_{4\mu} < 7.5$  GeV
  - ✓ The total background yields in the CR are used in the fit to constrain the background yields in the signal region

# Fit models in di-J/ $\psi$ channel

- In the di-J/ $\psi$  channel, two models are considered
  - **Model A** with three interfering S-wave resonances

$$f_s(x) = \left| \sum_{i=0}^2 \frac{z_i}{m_i^2 - x^2 - im_i\Gamma_i(x)} \right|^2 \sqrt{1 - \frac{4m_{J/\psi}^2}{x^2}} \otimes R(\theta)$$

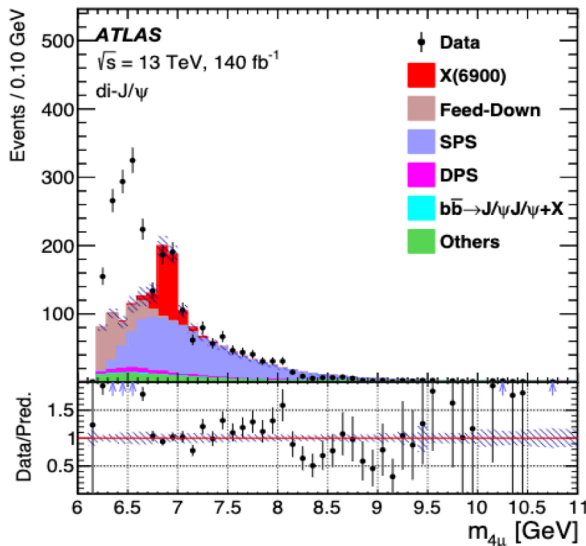
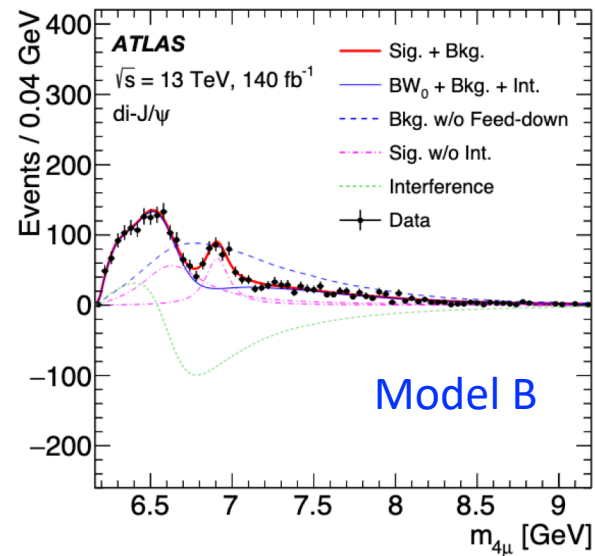
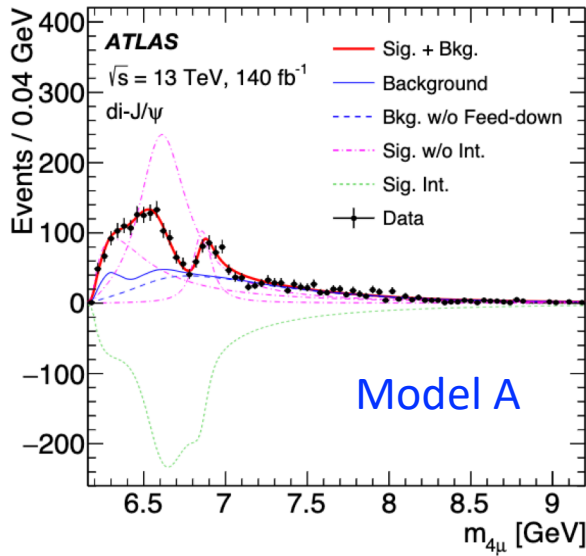
where  $z_1$  is fixed to unity with zero phase, and  $R$  is the mass resolution function that the BWs convolute with

- **Model B** with two S-wave resonances. The first interferes with SPS, while the second is standalone

$$f(x) = \left( \left| \frac{z_0}{m_0^2 - x^2 - im_0\Gamma_0(x)} + A(x)e^{i\phi} \right|^2 + \left| \frac{z_2}{m_2^2 - x^2 - im_2\Gamma_2(x)} \right|^2 \right) \sqrt{1 - \frac{4m_{J/\psi}^2}{x^2}} \otimes R(\theta)$$

where  $|A(x)|^2$  reproduces the non-interfering SPS background from the MC prediction

# Fit result in di- $J/\psi$ channel



di- $J/\psi$	model A	model B
$m_0$	$6.41 \pm 0.08^{+0.08}_{-0.03}$	$6.65 \pm 0.02^{+0.03}_{-0.02}$
$\Gamma_0$	$0.59 \pm 0.35^{+0.12}_{-0.20}$	$0.44 \pm 0.05^{+0.06}_{-0.05}$
$m_1$	$6.63 \pm 0.05^{+0.08}_{-0.01}$	—
$\Gamma_1$	$0.35 \pm 0.11^{+0.11}_{-0.04}$	—
$m_2$	$6.86 \pm 0.03^{+0.01}_{-0.02}$	$6.91 \pm 0.01 \pm 0.01$
$\Gamma_2$	$0.11 \pm 0.05^{+0.02}_{-0.01}$	$0.15 \pm 0.03 \pm 0.01$
$\Delta s/s$	$\pm 5.1\%^{+8.1\%}_{-8.9\%}$	—

# Fit models in $J/\psi+\psi(2S)$ channel

- In the  $J/\psi+\psi(2S)$  channel, two models are also considered
  - **Model  $\alpha$**  with two resonances. The first is the same as Model A in di- $J/\psi$  channel (parameters fixed), and second is standalone

$$f_s(x) = \left( \left| \sum_{i=0}^2 \frac{z_i}{m_i^2 - x^2 - im_i\Gamma_i(x)} \right|^2 + \left| \frac{z_3}{m_3^2 - x^2 - im_3\Gamma_3(x)} \right|^2 \right) \sqrt{1 - \left( \frac{m_{J/\psi} + m_{\psi(2S)}}{x} \right)^2} \otimes R(\theta)$$

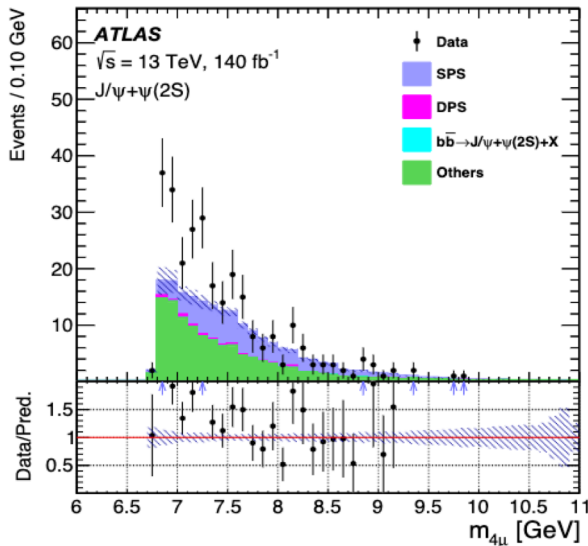
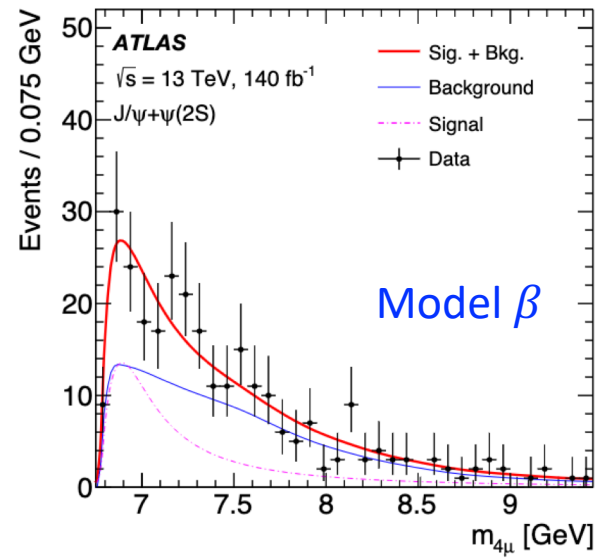
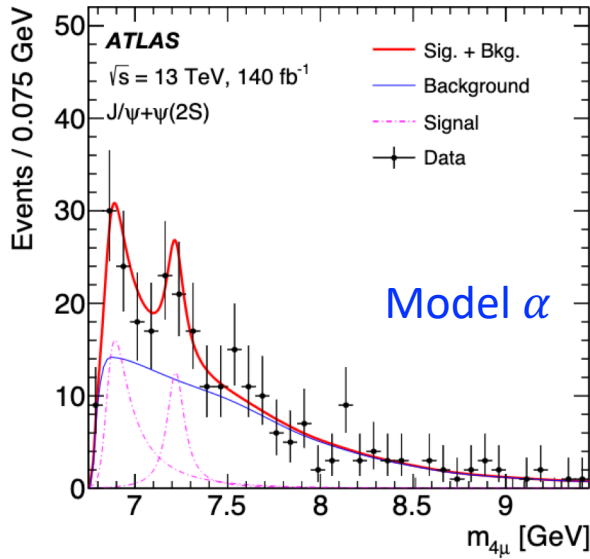
- **Model  $\beta$**  with a single resonance
- The feed-down background normalization is obtained as

$$N_{\text{fd}} = \frac{\mathcal{B}' \epsilon'}{\mathcal{B}(\psi(2S) \rightarrow \mu\mu) \epsilon} N$$

where  $\mathcal{B}' = [\mathcal{B}(\psi(2S) \rightarrow J/\psi + X) + \mathcal{B}(\psi(2S) \rightarrow \gamma\chi_{cJ}) \mathcal{B}(\chi_{cJ} \rightarrow \gamma J/\psi)] \mathcal{B}(J/\psi \rightarrow \mu\mu)$

Reconstruction systematics largely cancel each others in the ratio. The only significant systematics comes from the fitted error on signal yields  $N$  in the  $J/\psi+\psi(2S)$  channel

# Fit result in $J/\psi+\psi(2S)$ channel



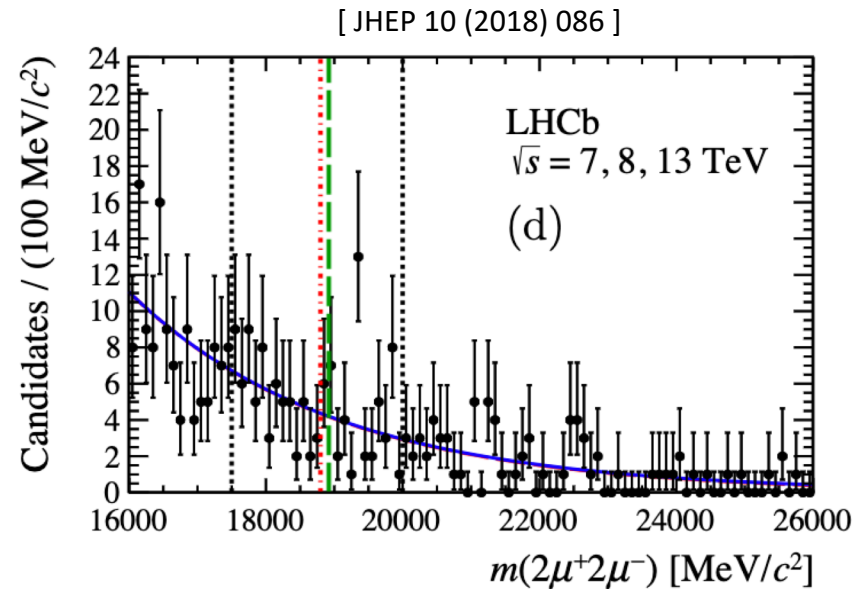
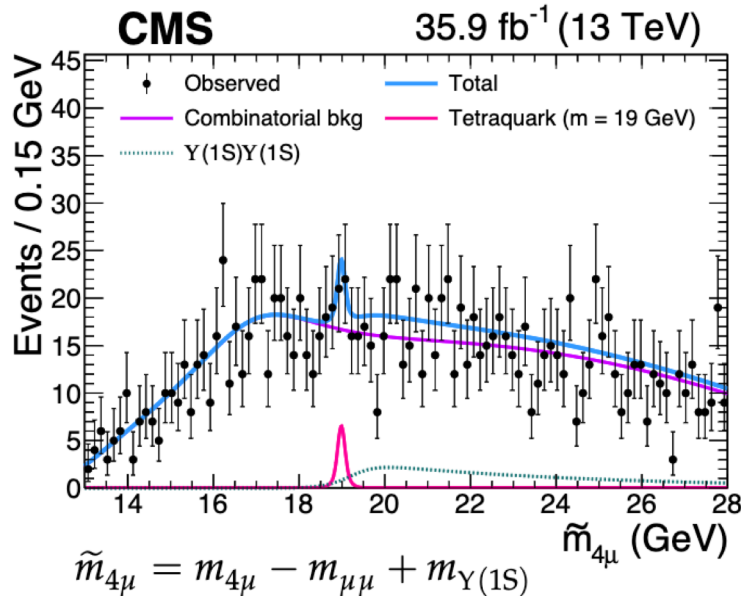
$J/\psi+\psi(2S)$	model $\alpha$	model $\beta$
$m_3$	$7.22 \pm 0.03^{+0.01}_{-0.04}$	$6.96 \pm 0.05 \pm 0.03$
$\Gamma_3$	$0.09 \pm 0.06^{+0.06}_{-0.05}$	$0.51 \pm 0.17^{+0.11}_{-0.10}$
$\Delta s/s$	$\pm 21\%^{+25\%}_{-15\%}$	$\pm 20\% \pm 12\%$

Total signal significance is  $4.7\sigma$  ( $4.3\sigma$ ) for Model  $\alpha$  ( $\beta$ ). In model  $\alpha$ , the significance of the second resonance alone is  $3.0\sigma$

# Full-beauty tetraquark?

- A tightly bound  $b\bar{b}b\bar{b}$  tetraquark state can have a mass below the threshold of  $\eta_b\eta_b$ , and decays to  $\Upsilon(1S) + \mu^+\mu^- \rightarrow 4\mu$ . This possible full-beauty tetraquark has been searched by ATLAS and other experiments (while other theoretical interpretations, e.g. a BSM Higgs, is also feasible)
- A potential resonance in the  $\Upsilon(1S) + \mu^+\mu^-$  channel have not been established by CMS and LHCb. It deserves a further check at ATLAS

[ Phys. Lett. B 808 (2020) 135578 ]



# Baseline cuts

[ ATLAS-CONF-2023-041 ]

- Baseline event selections for the  $\Upsilon(1S) + \mu^+ \mu^-$  search at ATLAS:

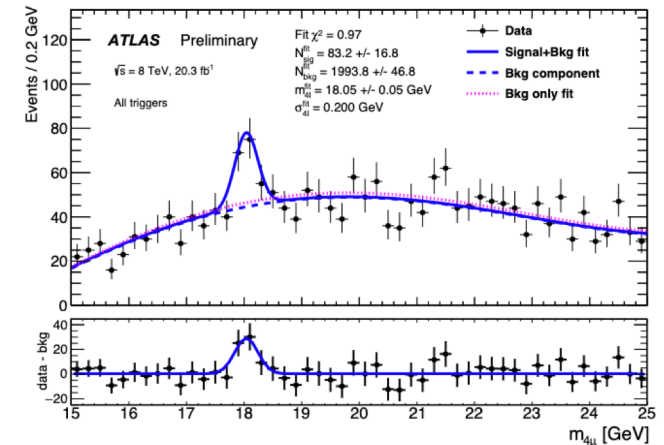
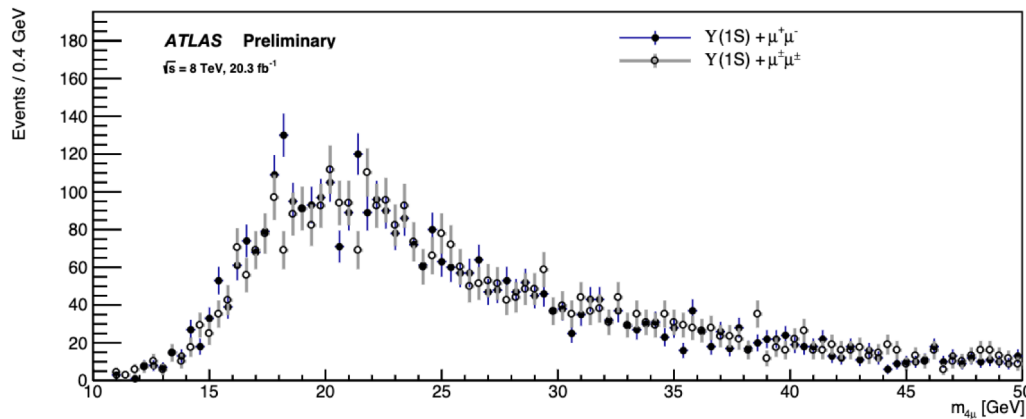
Candidate object	Requirements
Muons	$p_T(\mu) > 3$ GeV and $ \eta  < 2.5$ , $ z_0 \sin \theta  < 1$ mm and $ d_0/\sigma_{d_0}  < 6$
Muon quadruplet	$\geq 3$ muons passing LowPt selection criteria, $\sum q_\mu = 0$ , four-muon vertex fit $\chi^2/N_{\text{d.o.f}} \leq 10$ , $10$ GeV $\leq m_{4\mu} \leq 50$ GeV
Muon doublet	di-muon vertex fit $\chi^2 < 3$
$\Upsilon(1S)$ candidate	OS muon doublet with $p_T(\mu_{1,2}) > 4$ GeV, $9.2$ GeV $\leq m_{\mu^+\mu^-} \leq 9.7$ GeV
$\Upsilon(1S) + \mu^+ \mu^-$ candidate events	$\Upsilon(1S)$ candidate plus OS muon doublet with $m_{\mu^+\mu^-} > 1$ GeV, both muon doublets point to a common PV

- The background is modelled by a 4th-order Chebyshev polynomial and the signal by a Gaussian with its width fixed to the detector resolution ( $\sim 0.2$  GeV).
- Since the run-1 data did not follow a blind/unblind procedure, various modified selections w.r.t. the baseline cuts are applied to check the stability of the peak around 18 GeV (backup)

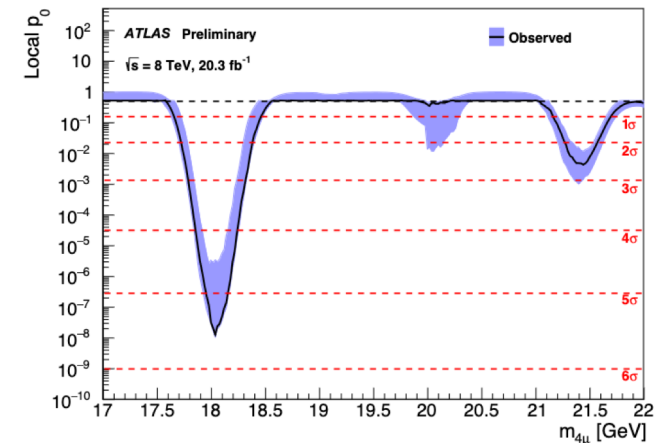


# $\Upsilon + \mu\mu$ search with 8 TeV run-1 data

- In 8 TeV run-1 data, three potential peaks are found at about 18.05 GeV, 21.4 GeV, and 31.7 GeV with local significances of 5.5, 2.4, and 2.6  $\sigma$

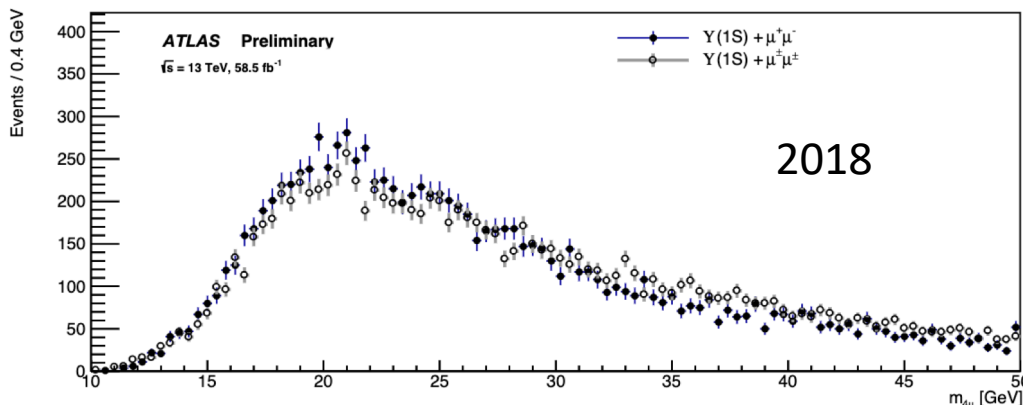
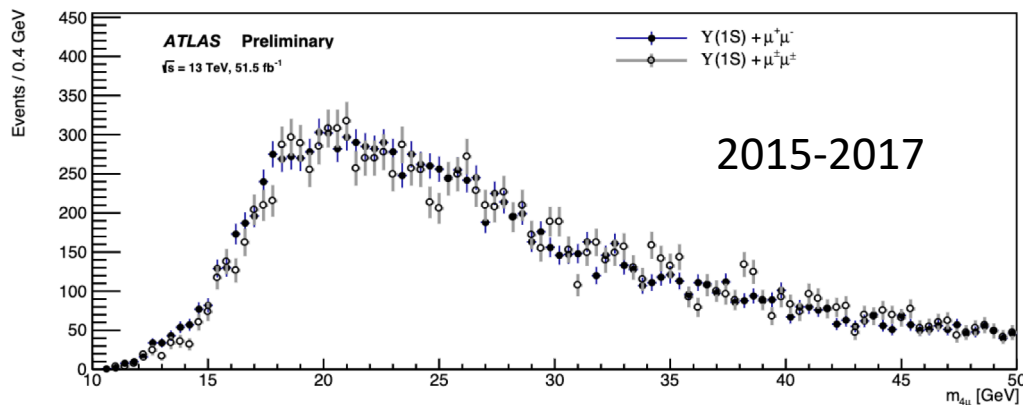


- To check if the peaks are artificial due to selection cuts, SS muons sample,  $m_{\mu\mu}$  mass sideband control samples,  $\Upsilon$ +di-track and single-muon + 3tracks data, event-mixed data, are investigated. No artificial structures are found in these checks



# $\Upsilon + \mu\mu$ search with 13 TeV run-2 data

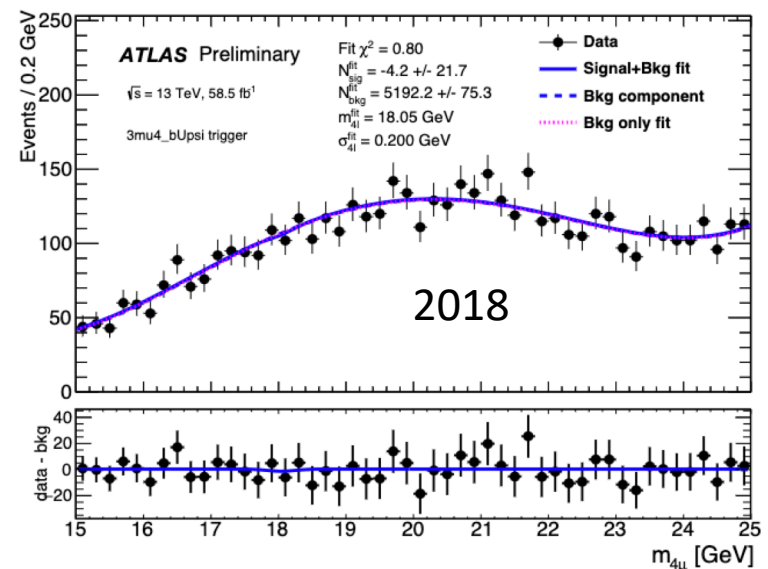
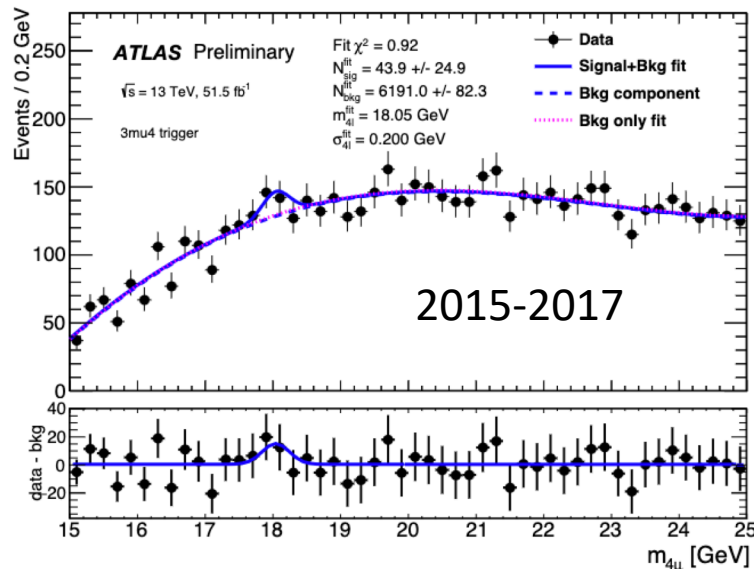
- Selection cuts for 13 TeV run-2 data were restricted to those used for the 8 TeV data. It serves as an independent check of the observed peaks in run-1



- In run-1, both di-muon and tri-muon triggers are used. No charge or mass requirements are imposed in the latter
- In run-2 data in years 2015-2017, similar trigger as run-1. But in run-2 2018, charge and mass cuts were required, which cause a shape difference in the OS vs SS  $m_{4\mu}$  distribution

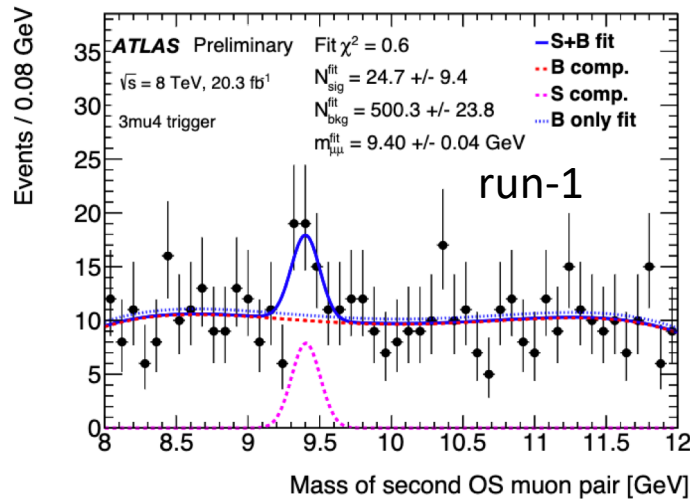
# $\Upsilon + \mu\mu$ search with 13 TeV run-2 data

- Signal yields around 18 GeV are much smaller than in run-1, so the Gaussian width is fixed to 0.2 GeV, and the mass in 2015-2017 (2018) is floated (fixed to 18.05 GeV)
- Fitted signal yields are  $48 \pm 25$  and  $-4 \pm 22$  in the two periods, while the backgrounds are  $\sim 2.5$  times larger per unit integrated luminosity in run-2 than in run-1

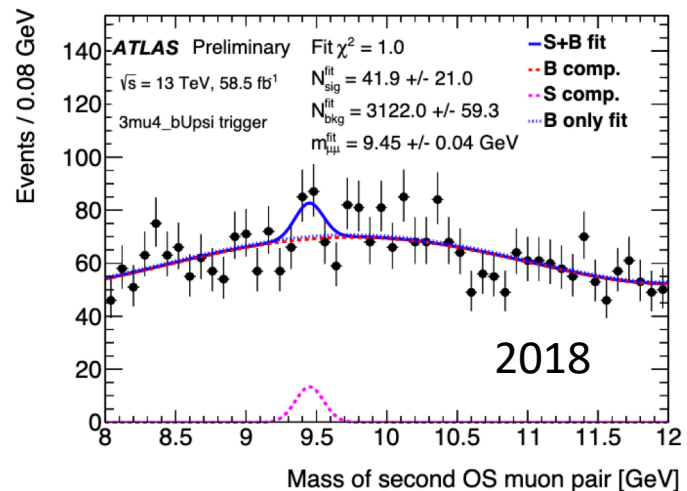
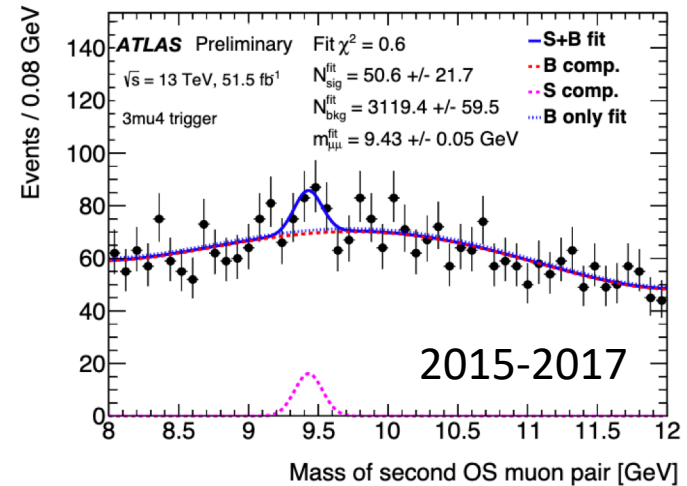


# $\Upsilon + \mu\mu$ search with 13 TeV run-2 data

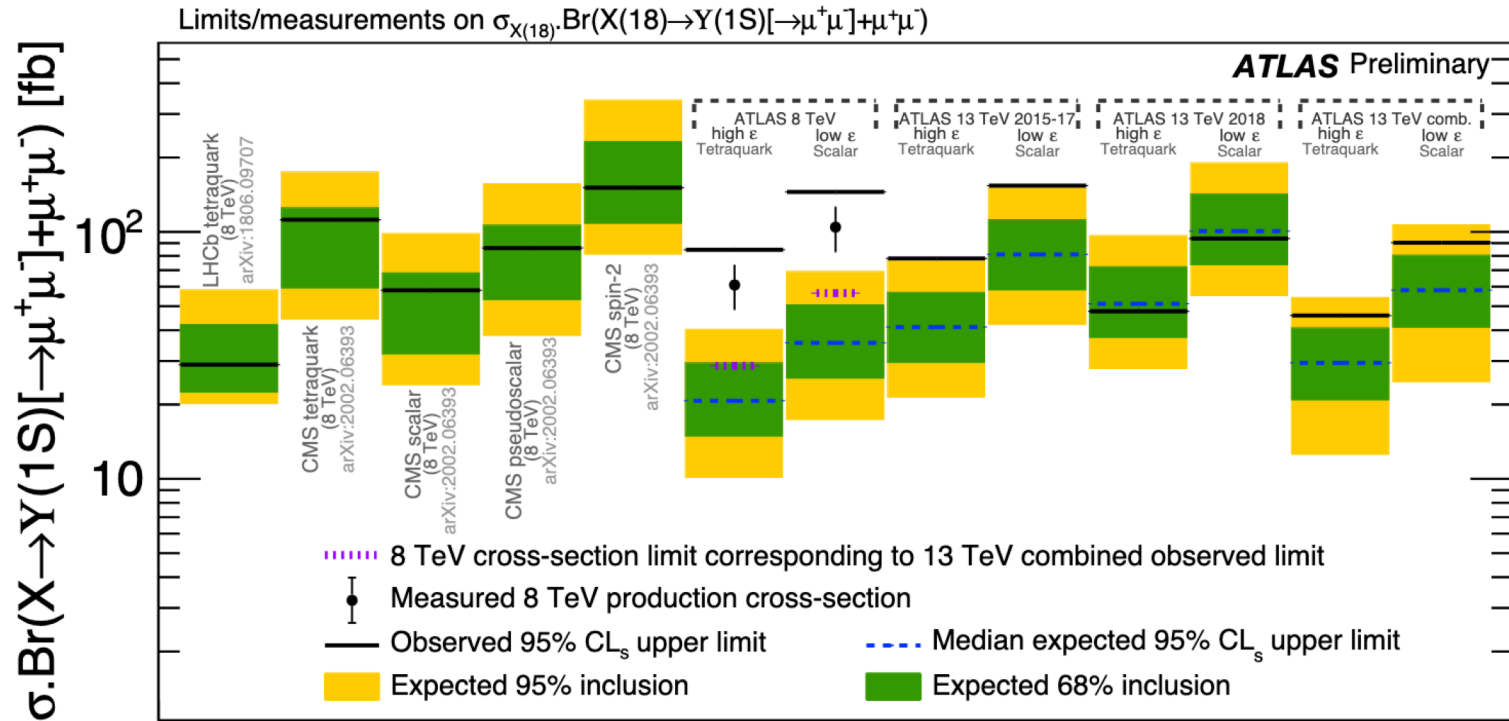
- With other things equal and assuming  $\frac{\sigma_{13\text{TeV}}}{\sigma_{8\text{TeV}}} = 1.4$ , the expected signal yield in 2015-2017 (2018) data is 89 (101), whereas the fitted signal yield is  $51 \pm 22$  ( $42 \pm 21$ )



- Similar trend is observed in the di- $\Upsilon$  data. The observed yield in run-2 is  $\sim 60\%$  of what would be expected if extrapolating from run-1 8 TeV data



# $\Upsilon + \mu\mu$ search limits



- $\text{CL}_s$  limits on  $\sigma \times \text{BR}$  of the 18 GeV peak are calculated with different signal models: 'Low  $\epsilon$ ' and 'high  $\epsilon$ ' refer to the limits derived from signal models with lowest (Higgs-like scalar) and highest (pseudoscalar tetraquark) predicted selection plus reconstruction efficiencies, respectively
- Further study with increased statistics from Run-3 data is needed

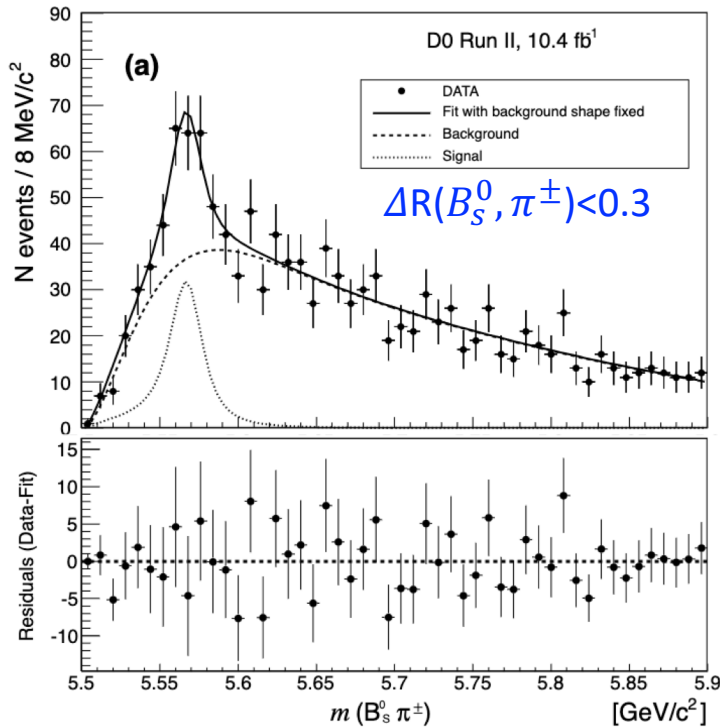
# Summary

- ATLAS is not only a discovery machine for high energy physics, but can also make low energy hadron measurements owing to its excellent tracking
- Hadron colliders are important for new hadron searches and for understanding QCD. New states should better be checked in different experiments. For example, the potential 18 GeV peak in  $\Upsilon + \mu\mu$  has not been established by ATLAS (and not by LHCb and CMS either)
- ATLAS searched for potential  $cc\bar{c}\bar{c}$  tetraquarks decaying into a pair of  $J/\psi$ 's, or into  $J/\psi + \psi(2S)$ , in the  $4\mu$  final state
  - ✓ Two models are used to fit the significant excess in the di- $J/\psi$  channel, one of which is consistent with  $X(6900)$  by LHCb and CMS
  - ✓ Two models are used to fit the excess in the  $J/\psi + \psi(2S)$  channel. More data is needed to measure its parameters
- We look forward to new results combining Run-3 of LHC

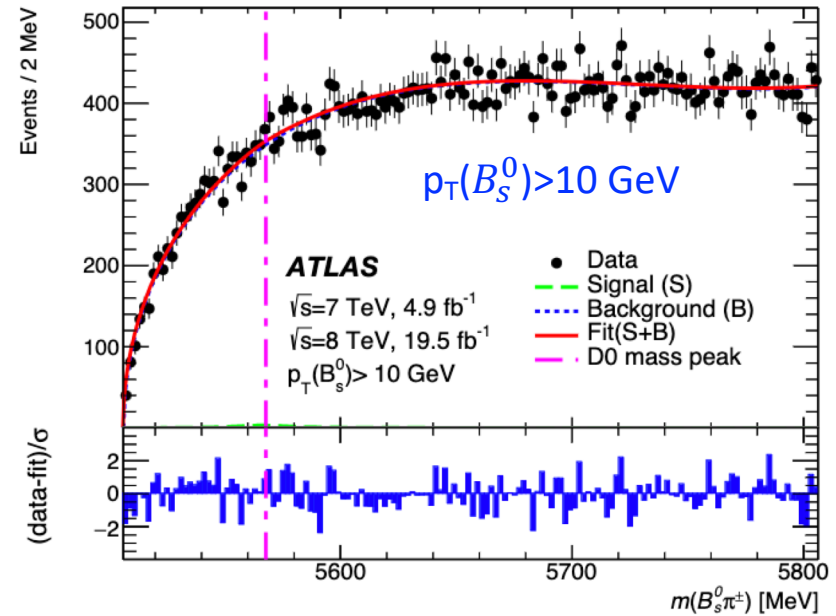
# Backup Slides

# $X^\pm(5568)$ from D0 and ATLAS

[ Phys. Rev. Lett. 117 (2016) 22003 ]



[ Phys. Rev. Lett. 120 (2018) 202007 ]



- In 2016, D0 claimed a potential resonance at about 5568 MeV in  $B_s^0 + \pi^\pm$  ( $5.1\sigma$ ), which is  $\sim 200$  MeV below  $B_d^0 + K^\pm$  and favors a tetraquark than a molecular interpretation
- However,  $X^\pm(5568)$  is not confirmed by ATLAS (neither by CMS or LHCb). Two main backgrounds are modelled separately – fake  $B_s^0$  (modelled by  $B_s^0$  sidebands) and random pions (modelled by MC with  $B_s^0$   $p_T$  tuned to data)



# $\Upsilon + \mu\mu$ search with 8 TeV run-1 data

- Since the run-1 data did not follow a blind/unblind procedure, various modified selections are applied to check the stability of the peak around 18 GeV

Selection criteria	$N_B$	Mass (GeV)	$N_S$	Significance ( $\sigma$ )
Baseline	$1994 \pm 47$	$18.05 \pm 0.05$	$83 \pm 17$	5.5
Selection variations from the baseline				
$\geq 2$ LowPt muons	$3124 \pm 59$	$18.09 \pm 0.06$	$94 \pm 20$	5.0
$= 4$ LowPt muons	$689 \pm 28$	$18.03 \pm 0.07$	$37 \pm 10$	4.1
$m_{\mu^+\mu^-}^{\text{non-res}} > 0$ GeV	$2515 \pm 53$	$18.00 \pm 0.06$	$81 \pm 19$	4.7
$m_{\mu^+\mu^-}^{\text{non-res}} > 0.5$ GeV	$2306 \pm 51$	$18.00 \pm 0.05$	$87 \pm 18$	5.3
$m_{\mu^+\mu^-}^{\text{non-res}} > 2$ GeV	$1696 \pm 43$	$18.05 \pm 0.07$	$58 \pm 15$	4.3
Vertex fit $\chi^2/N_{\text{d.o.f}} \leq 4$	$1705 \pm 43$	$18.03 \pm 0.05$	$69 \pm 15$	5.0
Vertex fit $\chi^2/N_{\text{d.o.f}} \leq 20$	$2077 \pm 48$	$18.04 \pm 0.05$	$81 \pm 17$	5.0
$m_{\Upsilon(1S)} \pm 2\sigma_m$ window	$3705 \pm 64$	$18.09 \pm 0.06$	$90 \pm 22$	4.5
$\Upsilon(1S)$ mass correction	$1998 \pm 47$	$18.02 \pm 0.08$	$64 \pm 17$	4.1
$m_{\mu^+\mu^-}^{\text{non-res}} < m_{\Upsilon(1S)}$	$1418 \pm 40$	$18.06 \pm 0.05$	$94 \pm 17$	6.3
$p_T > 2.5$ GeV non-res. muons	$2741 \pm 55$	$18.05 \pm 0.05$	$70 \pm 19$	4.1
$p_T > 4$ GeV non-res. muons	$982 \pm 33$	$18.06 \pm 0.08$	$35 \pm 11$	3.6
Tight IP cuts	$1469 \pm 40$	$18.01 \pm 0.05$	$71 \pm 15$	5.5
Lifetime $ \tau/\sigma_\tau  < 3$	$1873 \pm 45$	$18.04 \pm 0.05$	$86 \pm 17$	5.6
MBS $< 3$	$1749 \pm 44$	$18.05 \pm 0.04$	$83 \pm 16$	5.8

# Full heavy tetraquark

$$(cc)_3^* - (\bar{c}\bar{c})_3$$

$L$	$S$	$J^{PC}$	Mass (GeV)
1	0	$1^{--}$	6.55
	1	$0^{-+}, 1^{-+}, 2^{-+}$	
	2	$1^{--}, 2^{--}, 3^{--}$	
2	0	$2^{++}$	6.78
	1	$1^{+-}, 2^{+-}, 3^{+-}$	
	2	$0^{++}, 1^{++}, 2^{++}, 3^{++}, 4^{++}$	
3	0	$3^{--}$	6.98
	1	$2^{-+}, 3^{-+}, 4^{-+}$	
	2	$1^{--}, 2^{--}, 3^{--}, 4^{--}, 5^{--}$	

$$(cc)_6 - (\bar{c}\bar{c})_6^*$$

$L$	$S$	$J^{PC}$	Mass (GeV)
1	0	$1^{--}$	6.82
2	0	$2^{++}$	7.15
3	0	$3^{--}$	7.41



Fig. 2

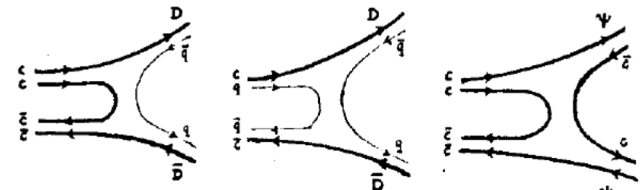


Fig.3(a)

Fig.3(b)

Fig.3(c)

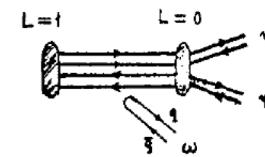


Fig. 4

- First mention of the 4c state (6.2 GeV, 1975): Prog. of Theo. Phys. Vol. 54, No. 2
- First calculation of the 4c mass (diquark+antidiquark): Z. Phys. C 7 (1981) 317

Full heavy tetraquark is different from heavy+light quark composition

# Maximum Likelihood

- Unbinned maximum likelihood fits are made to extract the signal information from data in the  $4\mu$  mass spectra
- The likelihood reads:

$$\mathcal{L} = \mathcal{L}_{SR}(\vec{\alpha}, \vec{\beta}) \cdot \mathcal{L}_{CR}(\vec{\alpha}) \cdot \prod_{j=1}^K G(\alpha'_j; \alpha_j, \sigma_j),$$

$$\mathcal{L}_{SR} = \frac{(s+b)^N}{N!} e^{-(s+b)} \prod_{i=1}^N \left[ \frac{s}{s+b} f_s(x_i; \vec{\alpha}, \vec{\beta}) + \frac{b}{s+b} f_b(x_i; \vec{\alpha}) \right], \quad \mathcal{L}_{CR} = \frac{b_{CR}^{N_{CR}}}{N_{CR}!} e^{-b_{CR}}, \quad \text{with } b_{CR} = b \cdot t(\alpha_t),$$

$\beta$  are the parameters of interest,  $\alpha$  are the nuisance parameters (NP) accounting for systematics shared between the two regions

- Each NP has a Gaussian constraint with a subsidiary measurement  $\alpha'_j$ , a mean  $\alpha_j$  and a width  $\sigma_j$
- In the di- $J/\psi$  channel, feed-down from  $J/\psi + \psi(2S)$  is included as an additional background

# Fit models

- The signal probability density function (PDF) consists of several interfering S-wave Breit-Wigner (BW) peaks convoluted with a mass resolution function

$$f_s(x) = \left| \sum_{i=0}^2 \frac{z_i}{m_i^2 - x^2 - im_i \Gamma_i(x)} \right|^2 \sqrt{1 - \frac{4m_{J/\psi}^2}{x^2}} \otimes R(\alpha),$$

- In general, the BW function for orbital angular momentum L is ( $F_L$  is the Blatt-Weisskopf form factor,  $R = 3 \text{ GeV}^{-1}$ )

$$BW(x; m_0, \Gamma_0) = \frac{\left(\frac{q}{q_0}\right)^L \frac{F_L(Rq)}{F_L(Rq_0)}}{m_0^2 - x^2 - im_0 \Gamma(x)}, \quad \Gamma(x) = \Gamma_0 \left(\frac{q}{q_0}\right)^{2L+1} \frac{m_0 F_L^2(Rq)}{x F_L^2(Rq_0)}.$$

- For S-wave, this is simplified to

$$BW(x; m_0, \Gamma_0) = \frac{1}{m_0^2 - x^2 - im_0 \Gamma(x)} = \frac{1}{m_0^2 - x^2 - im_0 \Gamma_0 \frac{m_0}{x} \sqrt{\frac{x^2 - 4m_{J/\psi}^2}{m_0^2 - 4m_{J/\psi}^2}}}$$

# Systematics

Since normalizations are freely floating, only systematics affecting the signal and background shapes are considered:

- muon momentum
- $J/\psi$  mass resolution
- MC simulation statistics
- SPS theory and di-charmonium  $p_T$
- background transfer factor
- “others” non-closure
- P and D-wave BW
- Feed-down

Systematic Uncertainties (MeV)	di- $J/\psi$		$J/\psi+\psi(2S)$	
	$m_2$	$\Gamma_2$	$m_3$	$\Gamma_3$
Muon calibration	$\pm 6$	$\pm 7$	$< 1$	$\pm 1$
SPS model parameter	$\pm 7$	$\pm 7$	$< 1$	
SPS di-charmonium $p_T$	$\pm 7$	$\pm 8$	$< 1$	
Background MC sample size	$\pm 7$	$\pm 8$	$\pm 1$	$< 1$
Mass resolution	$\pm 4$	$-3$	$-1$	$^{+2}_{-4}$
Fit bias	$-13$	$+10$	$^{+9}_{-10}$	$^{+50}_{-16}$
Shape inconsistency	$< 1$		$\pm 4$	$\pm 6$
Transfer factor	—		$\pm 5$	$\pm 23$
Presence of 4th resonance	$< 1$		—	
Feed-down	$^{+4}_{-1}$	$^{+6}_{-2}$	—	
Interference of 4th resonance	—		$-32$	$-11$
P and D-wave BW	$+9$	$+19$	$< 1$	$\pm 1$
$\Delta R$ and muon $p_T$ requirements	$^{+3}_{-2}$	$^{+6}_{-4}$	$^{+1}_{-2}$	$-2$
Lower resonance shape	—		$^{+3}_{-7}$	$^{+31}_{-34}$