

Assessment of Twitter Data Clusters with Cosine-Based Validation Metrics Using Hybrid Topic Models



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ABSTRACT

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Text data clustering is performed for organizing the set of text documents into the desired number of coherent and meaningful sub-clusters. Modeling the text documents in terms of topics derivations is a vital task in text data clustering. Each tweet is considered as a text document, and various topic models perform modeling of tweets. In existing topic models, the clustering tendency of tweets is assessed initially based on Euclidean dissimilarity features. Cosine metric is more suitable for more informative assessment, especially of text clustering. Thus, this paper develops a novel cosine based external and interval validity assessment of cluster tendency for improving the computational efficiency of tweets data clustering. In the experimental, tweets data clustering results are evaluated using cluster validity indices measures. Experimentally proved that cosine based internal and external validity metrics outperforms the other using benchmarked and Twitter-based datasets.

1. INTRODUCTION

Text clustering is used in many applications, including web mining, social data classification, fake news detection, etc. The critical challenging issue is to classify the text document without prior knowledge about the pre-cluster estimations [1]. Topics clustering [2] or topics based text document classification are the post clustering techniques. Topic models need prior knowledge about the cluster estimations. Authors of [3-6] presented the techniques for topic modeling of text documents for the clustering problem; however, these are underlying post text clustering techniques. State-of-the-art techniques focused on hybrid topic models [7] for the text clustering problem, which initially attempts to find the number of clusters and then finds the topics clusters of text documents.

Cluster validity measured with internal and external validity indices. The external validity indices [8-11] measure the correspondence between identified clusters and externally provided labels. The Internal validity indices [12-17] evaluate the goodness of cluster structure with partitioned data by considering compactness and separation of obtained partitioned structure. Internal validity indices are preferred in performance measures because, in most cases, prior information on the number of clusters will not be available. In previous literature, a wide variety of internal and external validity indices have been provided, which will help find the number of topics but not choose an appropriate measure, and metric to validate the cluster and not by considering the cluster elements well classified not. The most commonly used measure is Euclidean distance, which shows poor results in high dimensionality document clustering. In this paper, a novel cosine based internal and external validity metrics proposed for internally evaluating the results of a document clustering by considering into account the peculiarity of

textual data [18], the closeness between documents [19], considering the lexical similarity [20], and also considered cluster classification metrics in the classification of elements in the cluster are well classified or not. Experimentally evaluated the effectiveness of proposed cluster validity metrics with benchmark and Twitter-based datasets.

Overall summary of the research is described as follows:

1. Pre-cluster estimations of the tweets data are determined.
2. Topics clusters are determined for 2-Keyword phrases to 25-Keyword phrases of tweets dataset.
3. Cosine-based external and internal cluster metrics are used for the better evaluation of tweets data clustering.
4. Visual topic models are developed for the tweets data clustering.
5. Empirical evaluation is performed using validity indexes for the effective demonstration of the proposed method with cosine-based external and internal metrics.

2. THEORETICAL BACKGROUND OF CLUSTERING IN TOPIC MODELING

Different algorithms give different solutions for the same dataset by generating sub-clusters; different choice of input parameters produce different results for the same algorithm, which affects the final result in finding the optimal number of topics or clusters in the given topic document. To assess cluster obtained by used algorithm, to decide which algorithm is most suitable for the specific application, and to provide reliability to results suitable evaluation criteria under suitable measure is still needed. In most algorithms proximities, pairwise distances measured using Euclidean distance metrics are considered suitable for the lower number of dimensionality;

it loses its reliability and interpretability at an increase of dimensionality. Clustering algorithms deal with distance, and distance relates to similarity/dissimilarity. The complement to Euclidean metric is cosine-based similarity metric in text classification problems which uses both magnitude and direction of vectors, which is non-negative, independent of document length and bounded between [0, 1]. One of the most exciting variations in the K-means family is spherical k-means [21], which is based on cosine-based similarity used in information retrieval, in which the effect of different lengths of documents is reduced by normalization. Given two tweet documents d_i and d_j in a corpus, then cosine based distance similarity is given as

$$\cos(d_i, d_j) = \frac{d_i^T d_j}{\|d_i\| \cdot \|d_j\|} \quad (1)$$

The cosine is 1 if the documents use the same words and 0 if they have no two terms in common.

3. PROCESS DESCRIPTION AND CLUSTER VALIDATION

3.1 Datasets description

For the experiment, the datasets were collected from Twitter on 20 topics of health-related documents, TREC2014, TREC2015 Keyword Phrases. Tweets were collected from Twitter and the samples are described by Rajendra Prasad et al. [7], and Tweets extracted from Twitter related to 25 keyword phrases of TREC2018 [22] as described in Table 1. Experiments are implemented with Intel core i7 processor @3.4 GHz, 8MB cache, 16GB RAM, 1TB HDD in IDLE (Python 3.8 64bit) environment on these four different datasets and results discussed in ensuing sections.

Table 1. TREC2018 keyword phrases based tweets documents

S.No.	Datasets	Description of Keyword Phrases
1	2Keyword Phrases	Women in Parliaments, Black Bear Attacks
2	3Keyword Phrases	Description of 2 Keyword Phares and Airport Security
3	4Keyword Phrases	Description of 3 Keyword Phares, and Wildlife Extinction
4	5Keyword Phrases	Description of 4 Keyword Phares, and Health and Computer Terminals
5	6Keyword Phrases	Description of 5 Keyword Phares, and, human smuggling
6	7Keyword Phrases	Description of 6 Keyword Phares, and, transportation tunnel disasters
7	8Keyword Phrases	Description of 7 Keyword Phares, and transportation tunnel disasters, piracy
8	9Keyword Phrases	Description of 8 Keyword Phares, and hydrogen energy
9	10Keyword Phrases	Description of 9 Keyword Phares, and euro opposition
10	11Keyword Phrases	Description of 10 Keyword Phares, and mercy killing
11	12Keyword Phrases	Description of 11 Keyword Phares, and tropical storms
12	13Keyword Phrases	Description of 12 Keyword Phares, and women clergy

S.No.	Datasets	Description of Keyword Phrases
13	14Keyword Phrases	Description of 13 Keyword Phares, and college education advantage
14	15Keyword Phrases	Description of 14 Keyword Phares, and women driving in Saudi Arabia
15	16Keyword Phrases	Description of 15 Keyword Phares, and eating invasive species
16	17Keyword Phrases	Description of 16 Keyword Phares, and protect Earth from asteroids
17	18Keyword Phrases	Description of 17 Keyword Phares, and, diabetes and toxic chemicals
18	19Keyword Phrases	Description of 18 Keyword Phares, and, car hacking
19	20Keyword Phrases	Description of 19 Keyword Phares, and, social media and teen suicide
20	21Keyword Phrases	Description of 20 Keyword Phares, and federal minimum wage increase.
21	22Keyword Phrases	Description of 21 Keyword Phares, and eggs in a healthy diet
22	23Keyword Phrases	Description of 22 Keyword Phares, and email scams
23	24Keyword Phrases	Description of 23 Keyword Phares, and ethanol and food prices
24	25Keyword Phrases	Description of 24 Keyword Phares, and bacterial infection mortality rate.

3.2 Process description

On each collected corpus, as mentioned above, the following steps are implemented:

- Step1: For each Twitter-based dataset collected, preprocessing is performed using the Python Gensim library to prepare text documents for Document Clustering and classification.
- Step2: Programs implemented in Python to applying hybrid Topic models [7] under Cosine based and Euclidean distance-based measures.
- Step3: Document clustering and classification performed.
- Step4: Assessment of document cluster with confusion atrices [23] and classification metrics by using novel cosine-based internal and external validity metrics.
- Step5: Results compared with Euclideanmetrics with confusion matrices and classification metrics are done.

3.3 Performance of cluster validation

Topic modeling selection of appropriate method for implementation and assessment of clustering quality is still open challenges. Since the number of topics or clusters is not known ahead, the final results needed to be evaluated for cluster validation irrespective of the clustering model. To validate the cluster, external validation indices and internal validation indices are used. The Twitter dataset is created for the specified keyword phrased with ground truth label information. Externally validity indices are used both ground truth labels and predicted labels obtained by the cluster methods. Optimality of clustering algorithms are evaluated using external cluster validity indices based on the matching of ground truth and predicted cluster labels of tweet documents. In addition to these internal validations, indices evaluate cluster structure with partitioned data by considering compactness and separation of obtained partitioned structure. It measures intra-cluster homogeneity, inter-cluster separability, or both. In most of the application, preliminary information of the number of clusters is not available in such scenarios internal validation indices are best suited for cluster

validation. This paper presents both internal validity indices (C.A., NMI, Precision, Recall, and F-Score) and internal validity indices (DB, SI, XI, PCI, PEI, and SM) are used for performance evaluation. In addition to these validity indices, classification metrics are also used to check whether the cluster elements are well classified or not topic-wise.

4. PRELIMINARY EXPERIMENTAL EVALUATION AND PERFORMANCE OF VALIDATION MEASURES

Euclidean or cosine metrics find the proximities among the tweet's documents. Tweet documents having many terms in order to get the data sparsity problem. The topic models aim to derive the topics instead of the terms. Hence, finding proximities based on topics is to overcome the data sparsity problem since the number of topics is less than the number of terms of the documents. The proposed work finds the proximities-based topics instead of the terms to address the dimensionality problem in the case of text data clustering.

The experiment aims to compare the behavior of cosine based internal and external validity indices with Euclidean based indices. To perform a comparative study using different benchmark and real-time twitter-based datasets are collected. Four hybrid topic models [7] are implemented under Euclidean and cosine-based measures on each dataset. Results of the five external validity indices and six internal validity indices on every dataset have been calculated and tabulated, and a sample of compared results are shown in the form of

tables and graphs.

All datasets of external and internal validity indices under cosine and Euclidean are tabulated for four hybrid topic models. Some sample results are presented in tabular and graphical forms. In Table 2, External validity index (Cluster Accuracy) of 2 keyword phrases to 25 keyword phrases of TREC2018 datasets, and Table 3, all external and internal validity indices of the TREC2014 dataset are shown. These results interpreted that cosine based external and internal validity indices perform better than Euclidean in most keyword phrases. Mainly performs well when smaller keyword phrases, as keyword phrases size increases result in values decreasing under both metrics, but consistency is still maintained in case of cosine based metrics. Higher values of results are represented in bold format.

4.1 Document clusters validation by using cosine based Measures

Evaluating compactness and separation of formed clusters is usually a Euclidean measure deployed in previous studies and external validity indices in most cases. Using this measure may be inconsistent with the criterion for getting partition for a specific algorithm. In this paper, with this motivation, novel coined-based metrics are used in document clustering algorithms using hybrid topic models and used in validating formed clusters using these metrics. Besides, that clusters have high cohesion and are well distinguished, both compactness and separation are considered.

Table 2. Sample table of external validity index clustering accuracy (C.A.)

Tweets Dataset	CLUSTERING ACCURACY (CA)							
	EUCLIDEAN based				COSINE based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	0.850	0.575	0.500	1.000	0.800	0.675	0.500
3KPhrases	1.000	0.500	0.467	0.375	1.000	0.625	0.542	0.442
4KPhrases	0.888	0.644	0.494	0.356	0.931	0.625	0.481	0.394
5KPhrases	0.615	0.495	0.360	0.310	1.000	0.465	0.620	0.335
6KPhrases	0.521	0.408	0.329	0.338	0.767	0.454	0.383	0.342
7KPhrases	0.445	0.407	0.332	0.300	0.861	0.321	0.407	0.268
8KPhrases	0.644	0.644	0.644	0.644	0.813	0.316	0.397	0.288
9KPhrases	0.497	0.406	0.286	0.275	0.767	0.317	0.369	0.289
10KPhrases	0.538	0.353	0.273	0.223	0.593	0.280	0.383	0.288
11KPhrases	0.450	0.266	0.309	0.198	0.714	0.268	0.323	0.239
12KPhrases	0.456	0.350	0.319	0.210	0.679	0.329	0.425	0.231
13KPhrases	0.423	0.221	0.252	0.250	0.508	0.288	0.346	0.202
14KPhrases	0.373	0.261	0.239	0.220	0.645	0.252	0.377	0.213
15KPhrases	0.293	0.207	0.263	0.200	0.331	0.175	0.226	0.148
16KPhrases	0.411	0.253	0.263	0.223	0.570	0.295	0.377	0.220
17KPhrases	0.378	0.210	0.222	0.213	0.550	0.288	0.301	0.244
18KPhrases	0.310	0.265	0.275	0.193	0.515	0.258	0.403	0.206
19KPhrases	0.359	0.222	0.322	0.197	0.570	0.299	0.382	0.245
20KPhrases	0.343	0.235	0.213	0.210	0.524	0.275	0.421	0.205
21KPhrases	0.540	0.150	0.610	0.145	0.542	0.139	0.298	0.137
22KPhrases	0.472	0.148	0.501	0.150	0.482	0.135	0.310	0.147
23KPhrases	0.477	0.160	0.503	0.141	0.480	0.145	0.283	0.145
24KPhrases	0.477	0.148	0.485	0.142	0.478	0.143	0.316	0.142
25KPhrases	0.573	0.153	0.468	0.143	0.574	0.134	0.302	0.146

VN: Visual NMF VL: Visual LDA VLS: Visual LSI VPL: Visual PLSA

Table 3. TREC2014 dataset external and internal validity indices

TREC2014 C.A.	Cosine Based				Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	0.975	1.000	0.750	1.000	0.975	0.975	0.700
3KPhrases	1.000	0.908	1.000	0.483	0.983	0.891	0.983	0.483

4KPhrases	1.000	0.725	1.000	0.450	0.850	0.825	0.968	0.443
N.M.I.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	0.831	1.000	0.188	1.000	0.831	0.831	0.118
3KPhrases	1.000	0.716	1.000	0.090	0.929	0.687	0.929	0.076
4KPhrases	1.000	0.439	1.000	0.153	0.636	0.583	0.901	0.161
Precision (P)		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	1.000	1.000	0.794	1.000	1.000	1.000	0.814
3KPhrases	1.000	1.000	1.000	0.460	1.000	1.000	0.983	0.460
4KPhrases	0.993	0.993	1.000	0.441	0.670	0.670	0.968	0.486
Recall(R)		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	1.000	0.975	0.675	1.000	1.000	0.875	0.550
3KPhrases	1.000	1.000	1.000	0.458	1.000	1.000	0.983	0.458
4KPhrases	0.993	0.993	1.000	0.443	0.706	0.706	0.968	0.500
F-Score(F)		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	1.000	1.000	0.987	0.729	1.000	1.000	0.933	0.656
3KPhrases	1.000	1.000	1.000	0.458	1.000	1.000	0.983	0.458
4KPhrases	0.993	0.993	1.000	0.440	0.656	0.656	0.968	0.489
D.B.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.690	0.765	0.690	1.229	0.929	2.874	0.932	2.025
3KPhrases	1.306	1.567	1.316	4.108	1.845	2.110	1.878	5.976
4KPhrases	1.855	3.876	1.875	6.184	3.570	3.903	2.848	5.465
S.I.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.998	0.800	0.869	0.654	0.894	0.859	0.090	0.432
3KPhrases	0.983	0.557	0.165	0.145	0.764	0.470	0.153	0.524
4KPhrases	0.962	0.103	0.065	0.042	0.163	0.252	-0.04	0.243
X.I.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.038	1.807	0.065	1.616	1.970	1.235	3.60	1.638
3KPhrases	14.38	20.47	25.94	17.63	94.03	30.15	40.01	29.96
4KPhrases	0.547	0.151	1.366	4.651	481.16	33.10	155.6	210.9
P.C.I.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.998	0.929	0.998	0.938	0.922	0.947	0.944	0.927
3KPhrases	0.978	0.862	0.968	0.968	0.851	0.830	0.847	0.958
4KPhrases	0.953	0.712	0.934	0.905	0.738	0.684	0.770	0.872
P.E.I.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.003	0.130	0.006	0.099	0.140	0.101	0.106	0.116
3KPhrases	0.048	0.277	0.073	0.064	0.286	0.337	0.294	0.082
4KPhrases	0.107	0.585	0.154	0.199	0.534	0.641	0.475	0.256
S.M.		Cosine Based			Euclidean Based			
	VN	VL	VLS	VPL	VN	VL	VLS	VPL
2KPhrases	0.025	0.038	0.0269	0.032	0.084	0.039	0.089	0.036
3KPhrases	0.022	0.046	0.0259	0.025	0.093	0.056	0.095	0.026
4KPhrases	0.022	0.054	0.0269	0.026	0.556	0.076	0.153	0.028

VN: Visual NMF VL: Visual LDA VLS: Visual LSI VPL: Visual PLSA

Consider corpus $X=\{d_1, d_2, \dots, d_n\} \subset K^p$ consists of n document vectors in 'p' terms space of dimension. With the help of a hybrid clustering algorithm, k number of clusters C_q (where $q=1, 2, \dots, k$) have been identified, such that each document has one of the labels identifying the k different clusters. These clustering algorithm aims to maximize intra-cluster proximities and minimize inter-cluster proximities. Let d_i, d_i' , and d_j be three documents in a corpus X , with d_i , and d_i' belongs to the same cluster, and d_j belongs to other clusters. Compactness and separation can be calculated as follows:

$$\text{Compactness } (C_q) = \sum_{d_i, d_i' \in C_q} \text{proximities}(d_i, d_i') \quad (2)$$

$$\text{Separation } (C_q, C_{q'}) = \sum_{\substack{d_i \in C_q \\ d_j \in C_{q'}}} \text{proximities}(d_i, d_j) \quad (3)$$

where proximities (.) usually the Euclidean distance.

In this paper, external validity indices Clustering Accuracy (CA), Normalized Mutual Information (NMI), Precision (P), Recall (R) and F-Score (F) [24, 25] under cosine based metrics and derived internal validity indices with cosine similarity as mentioned below i.e. Davis-Bouldin Index (DB), Silhouette Index (SI), Partition Coefficient Index (PCI), Partition Entropy Index (PEI) and Separation Measure (SM) are considered for evaluating. In internal validity indices, the Davis-Bouldin index (D.B.) depends on both data and algorithm is given as:

$$DB = \frac{I}{N} \sum_{i=1}^N D_i \quad (4)$$

where, $D_i = \max_{j \neq i} R_{ij}$ and $R_{ij} = \frac{S_i + S_j}{M_{ij}}$.

Eq. (4) can be rewritten with cosine dissimilarity as:

$$DB_{\text{cosine}} = \frac{1}{N} \sum_{i=1}^N (1 - \cos(D_i)) \quad (5)$$

Silhouette index (S.I.) is given as

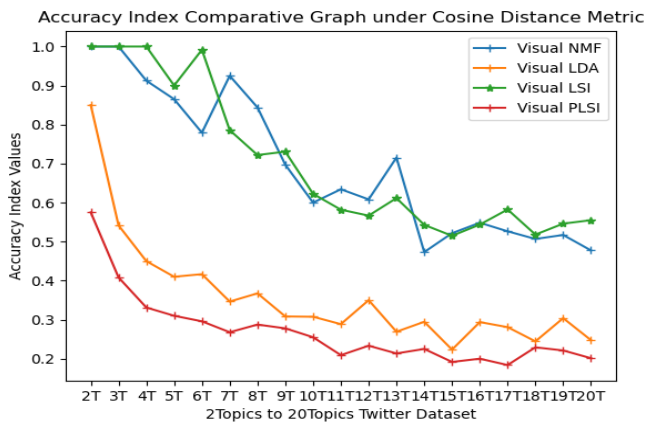
$$S(i) = \begin{cases} 1 - \frac{a(i)}{b(i)} & \text{if } a(i) < b(i) \\ 0 & \text{if } a(i) = b(i) \\ \frac{b(i)}{a(i)} - 1 & \text{if } a(i) > b(i) \end{cases} \quad (6)$$

By considering cosine similarity Eq. (6) can be written as

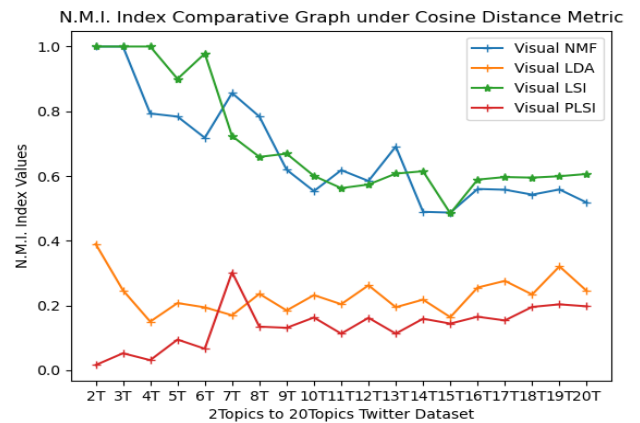
$$S(i)_{\text{cosine}} = \begin{cases} 1 - \cos\left(\frac{a(i)}{b(i)}\right) & \text{if } a(i) < b(i) \\ 0 & \text{if } a(i) = b(i) \\ \cos\left(\frac{b(i)}{a(i)} - 1\right) & \text{if } a(i) > b(i) \end{cases} \quad (7)$$

By using these equations, calculated values of validity indices are tabulated. Higher values are represented in the bold form in the tables mentioned below. These tabulated values show a comparison between cosine and Euclidean represented in graphical form in the following sections.

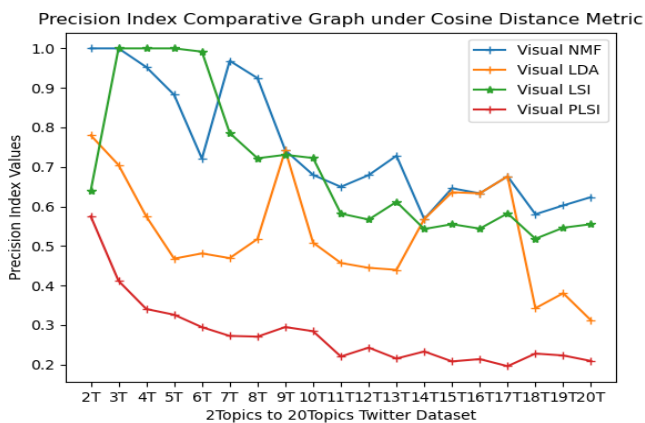
Graphical representation of experimental results of External and Internal Validity indices under cosine based.



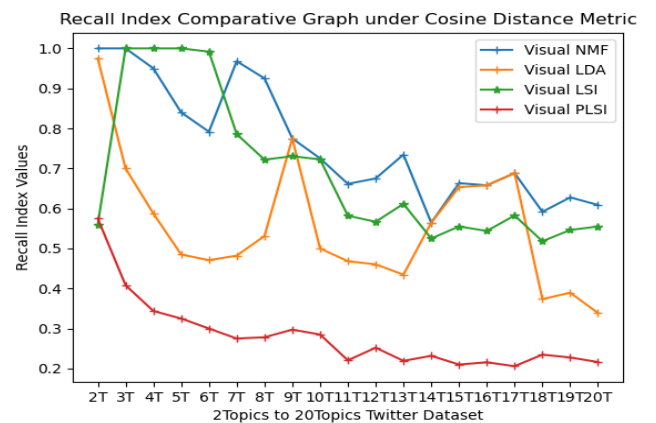
(a) Accuracy



(b) N.M.I.



(c) Precision



(d) Recall

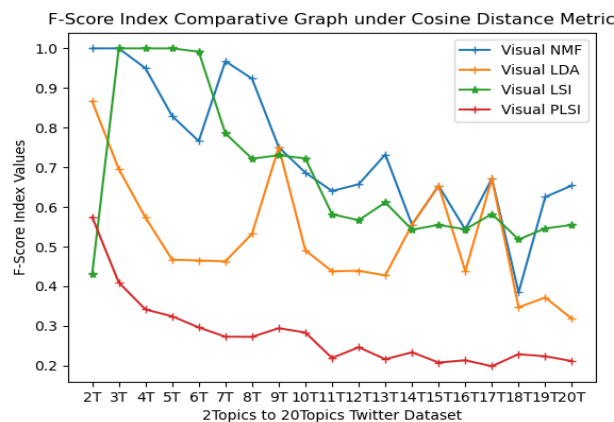


Figure 1. External validity indices of 2Topics to 20Topics Twitter dataset under cosine metric

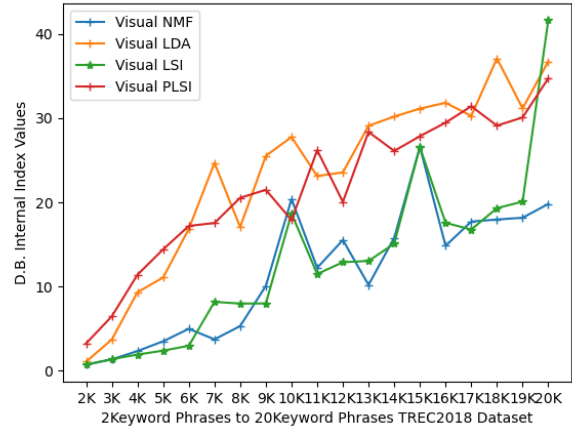
External validity indices (CA, NMI, Precision, Recall, and F-Score) under cosine of 2topics to 20 topics health datasets are represented as spiral graphs shown in Figure 1(a) to 1(e). All external validity indices values lies [0, 1]. Any external validity index value near value 1 performs better clustering. From Figure 1(a), Accuracy index results for 2topics to 20 topics are shown, from this spiral graph interpreted that Visual NMF and Visual LSI algorithm perform well. At 7T, 8T, 11T, and 12T visual NMF performs better than the other three methods. By observing NMI external index results shown in Figure 1(b) for most of the topics Visual LSI method performs well, whereas, for 7T, 8T, 11T, and 13T Visual NMF performance are better than other methods. In Figure 1(c) precision values are shown, from this inferred Visual NMF performs well in most of the topics except 3T to 6T, and 10T Visual LSI performs well. Recall values are shown in Figure 1(d) from which conclusion drawn except for 3T to 6T, for the rest of the topics Visual NMF performance is good. In those topics, Visual LSI performs well. In Figure 1(e) F-Score values are represented from these results inferred that both Visual NMF and Visual LSI perform well when compared to the other two methods for all five external indices values under cosine based metric.

Figure 2(a) shows the performance of Davis-Bouldin (DB) internal index values under the cosine metric of TREC2018 keyword phrases. Its values range from 0 to 40 shown on the Y-axis. In the case of this index, the minimum value will perform better clustering results. From this graph on observation, visual LSI performs better for most of the keyword phrases than other methods. In the case of 7keywords, 8keywords, 13keywords, 16keywords, 19keywords, and 20keywords Visual NMF performed better than other methods.

Silhouette index (SI) values range from -1 to +1. If this index value is nearer to +1 then cluster performance will be best. If values decrease from +1 to -1 its performance also decreases. From the bar graph shown in Figure 2(b) results can interpret Visual NMF under cosine performs well in all TREC2018 keyword phrases.

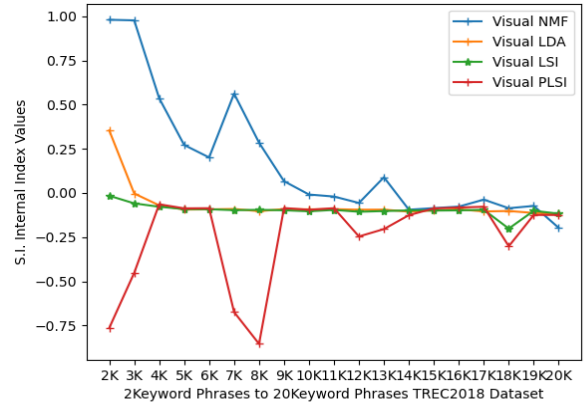
In Figure 2(c) Xie-Beni index (XI) internal validity index values under the cosine metric are represented. Its values range from 0 to 110 as represented on the Y-axis. The minimum value of this index will be considered as the best performance. From this line graph, in the case of 3keyword phrases, Visual LDA performs better than other methods; in the rest of the keyword phrases, Visual PLSI performed better than other methods.

D.B. Internal Index Comparative Graph under Cosine Distance Metric



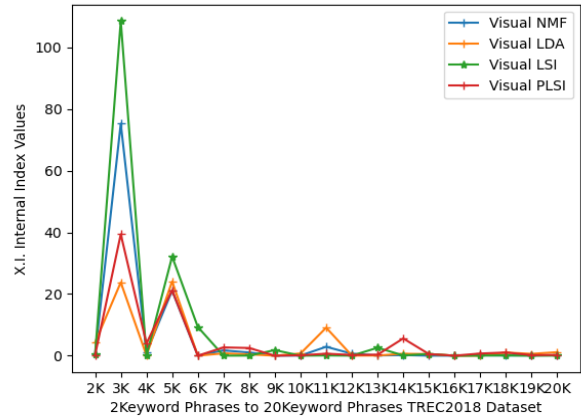
(a) Davies-Bouldin Index (D.B.)

S.I. Internal Index Comparative Graph under Cosine Distance Metric



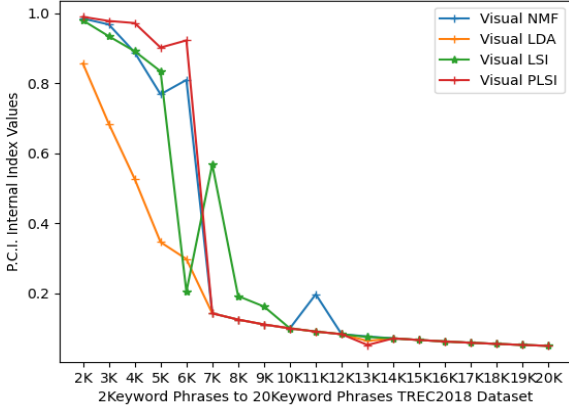
(b) Silhouette Index (SI)

X.I. Internal Index Comparative Graph under Cosine Distance Metric



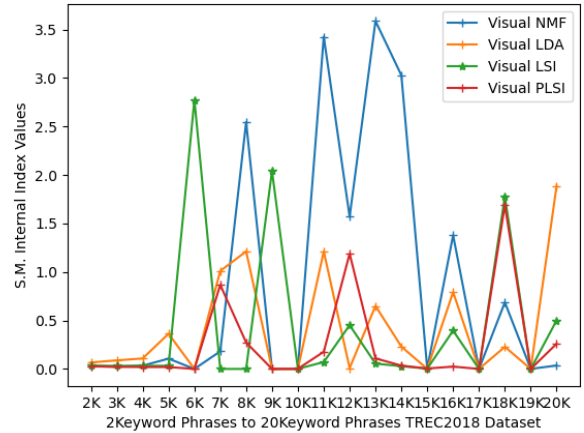
(c) Xie-Beni Index (XI)

P.C.I. Internal Index Comparative Graph under Cosine Distance Metric



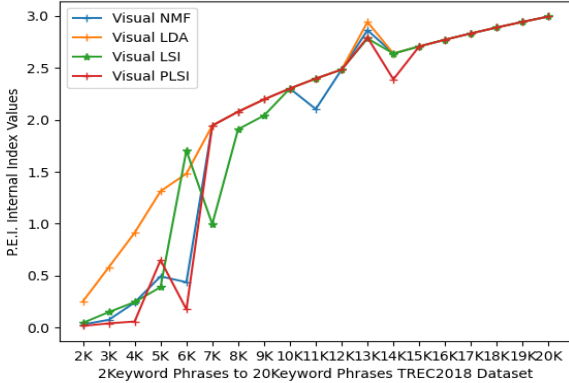
(d) Partition Coefficient Index (PCI)

S.M. Internal Index Comparative Graph under Cosine Distance Metric



(f) Separation Measure (SM)

P.E.I. Internal Index Comparative Graph under Cosine Distance Metric



(e) Partition Entropy Index (PEI)

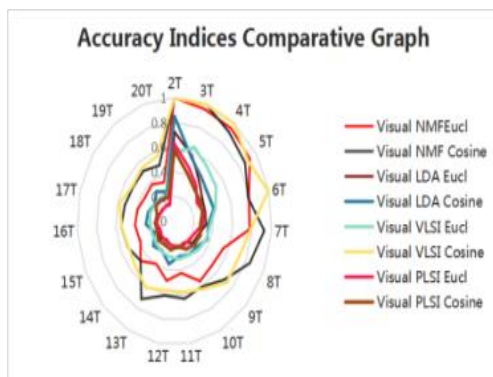
Figure 2. TREC2018 Dataset Internal Validity Indices under cosine Metric

Partition coefficient index (PCI) values lie between 0 and 1. Values nearer to 1 will be treated as best. From Figure 2(d), based on PCI values under cosine metric, in the case of 7 keyword phrases and ten keywords, Visual LSI performs better, for 11 keyword phrases Visual NMF performs well, and in the rest of all keyword phrases, Visual PLSI methods perform well.

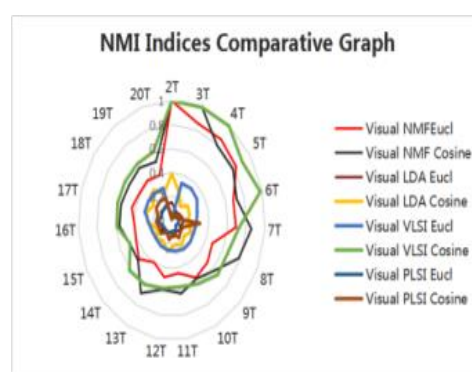
Figure 2(e) shows performance values of partition coefficient internal index values, which range from 0 to $\log c$. In this case, its value range from 0 to 3, as indicated on the Y-axis line graph. The minimum value will be considered for higher performance in clustering. From this graph, the Visual LSI method performs well for 7 to 10 keyword phrases, for 11 and 12 keyword phrases Visual NMF and for the rest of keyword phrases Visual PLSI performs better than other methods.

Separation Measure internal index value is smaller then it will have more excellent performance. In this case, its value ranges from 0 to 10 as represented on the Y-axis. This line graph shows in Figure 2(f), 7 keyword phrases, 8 keywords, 11 keywords, and 13 keywords Visual LSI performs well and in the rest of keyword phrases, Visual PLSI under cosine metric performs better than other methods.

4.2 Comparative study of cosine based validation with Euclidean distance-based cluster validation



(a) Accuracy



(b) N.M.I.

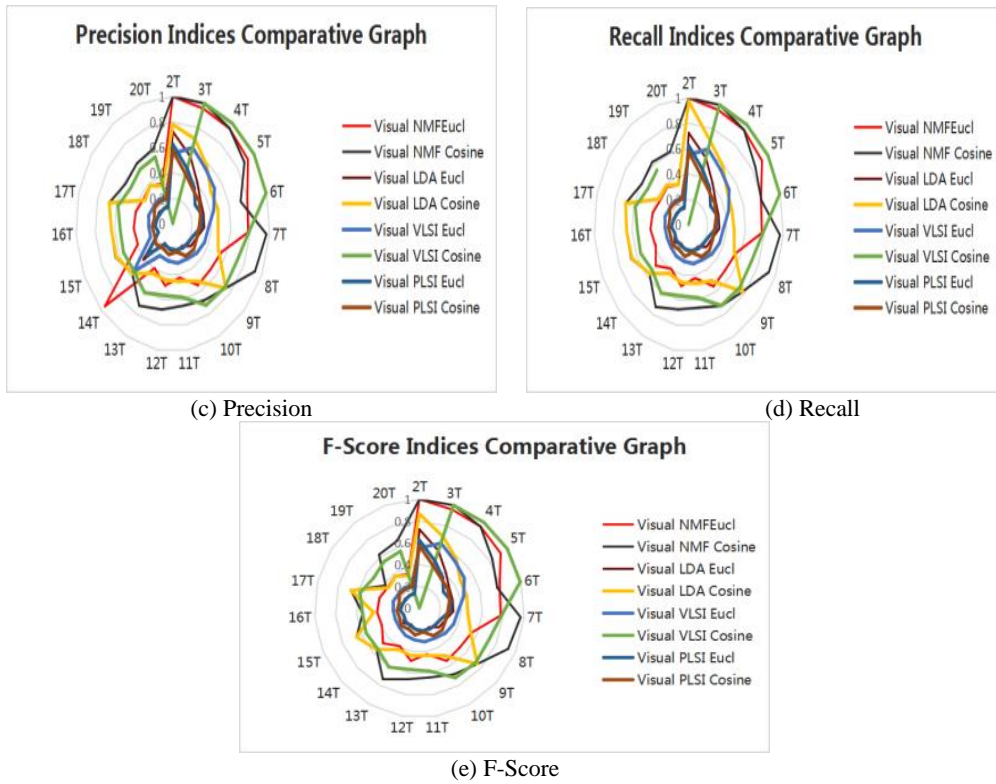


Figure 3. External validity indices Comparative results of 2Topics to 20Topics Twitter Dataset

External validity indices (CA, NMI, Precision, Recall, and F-Score) comparative results of 2topics to 20 topics health datasets are represented in the form of spiral graphs as shown in Figure 3(a) to 3(e). All external validity indices values lies [0, 1]. Any external validity index value near value 1 performs better clustering. From Figure 3(a) Accuracy index results for 2topics to 20 topics are shown, from this spiral graph Visual LSI algorithm under cosine based metric performs well. At 7T, 8T, 11T, and 12T visual NMF under cosine perform better than the other three methods. By observing NMI external index results in Figure 3(b) for most of the topics Visual LSI under cosine metric performs well, whereas, for 7T, 8T, 11T, and 12T Visual NMF under cosine performance are better than other methods. In Figure 3(c) precision values are shown, from this results inferred Visual LSI under cosine metric performs well in most of the topics except 7T, 8T, 12T, and 13T Visual NMF under cosine perform, whereas at 14 Visual NMF under Euclidean perform well when compared to all other methods. Recall values are shown in Figure 3(d) from which the conclusion is drawn that both Visual NMF and Visual LSI under cosine metric perform equally. In Figure 3(e) F-Score values are represented from this can inferred that both Visual NMF and Visual LSI under cosine metric perform well. On overall performance, both Visual NMF and Visual LSI under cosine metric perform well when compared Euclidean for all five external indices value.

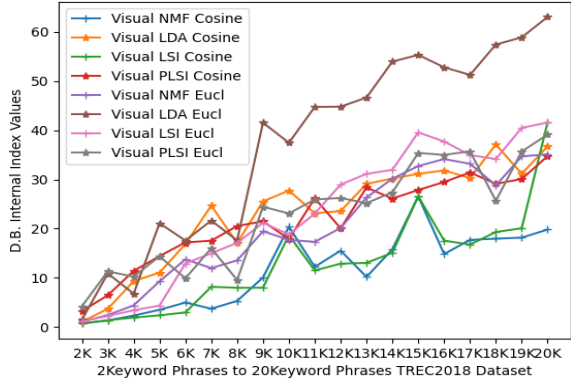
Figure 4(a) shows comparative performance results of Davis-Bouldin (DB) internal index values under Cosine and Euclidean metrics of TREC2018 keyword phrases. Its values range from 0 to 70 shown on the Y-axis. In the case of this index, the minimum value will be considered for better clustering results. Form this graph on observation, 2keywords to 6keywords, 9keywords to 12keywords, 14keywords and 17keywords visual LSI under cosine perform well, for 18keyword phrases visual NMF performs best and rest of keyword phrases Visual NMF under Cosine performs better than other models. Silhouette index (SI) values range from -1

to +1. If this index value is nearer to +1 then cluster performance will be best. If values decrease from +1 to -1 its performance also decreases. From the line graph as shown in Figure 4(b) interpreted that Visual NMF under cosine performs well in all TREC2018 keyword phrases, except 5keyword phrases where Visual NMF under Euclidean performs well.

In Figure 4(c) Xie-Beni index (XI) internal validity index values under cosine and Euclidean metric are represented. Its values range from 0 to 110 as represented on the Y-axis. The minimum value of this index will be considered as the best performance. From this line graph, in the case of 2keyword phrases to 5keyword phrases, visual LDA under Euclidean performs well, and the rest of the keyword phrases of TREC2018 datasets visual PLSI under Cosine metric performs better than other methods and also better than Euclidean distance metric.

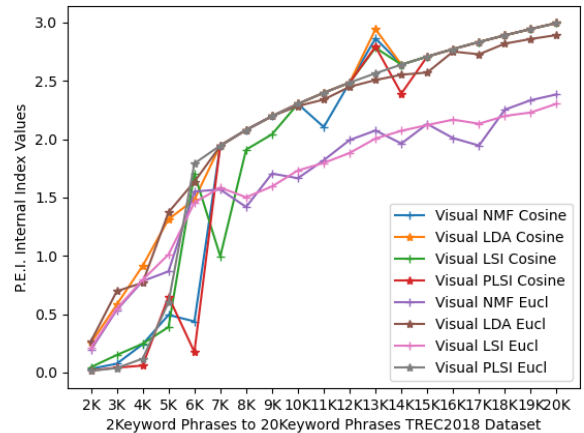
Partition coefficient index (PCI) values lie between 0 and 1. Maximum values will be considered as better performance; values nearer to 1 will be treated as best. From Figure 4(d), based on PCI comparative result values under Cosine and Euclidean metrics, interpret that 2keyword phrases to 6keyword phrases visual PLSI under cosine metric performance is good, for 8keywords, 10keywords, 14keywords, and 17keyword phrases visual NMF under Euclidean metric, and for the rest of keyword phrases, visual LSI under Cosine metric performs well.

D.B. Internal Index Comparative Graph of TREC2018 Dataset



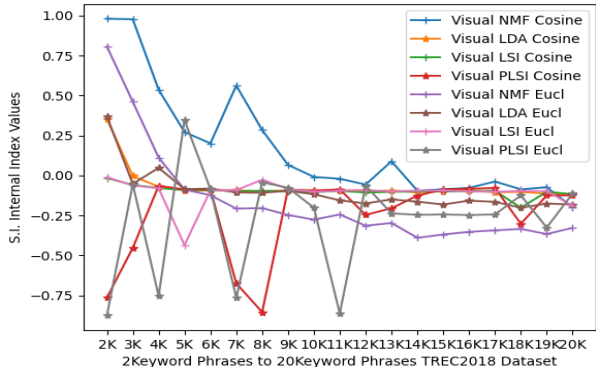
(a) Davies-Bouldin index (D.B.) comparative results

P.E.I. Internal Index Comparative Graph of TREC2018 Dataset



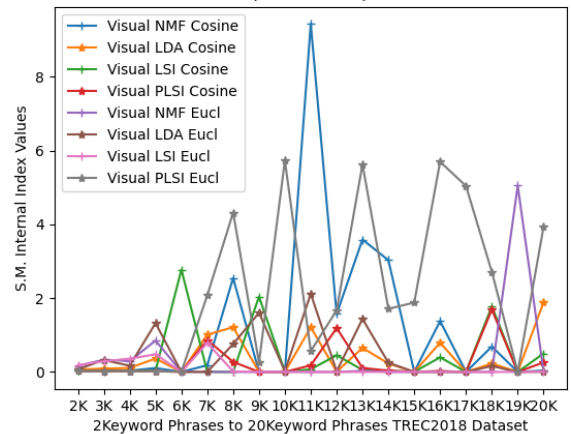
(e) Partition entropy index (PEI) comparative results

S.I. Internal Index Comparative Graph of TREC2018 Dataset



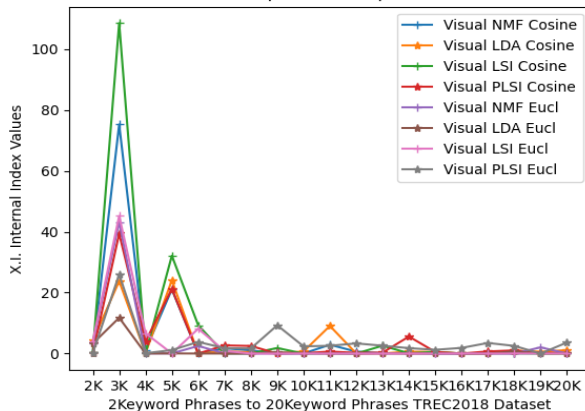
(b) Silhouette index(SI) comparative results

S.M. Internal Index Comparative Graph of TREC2018 Dataset



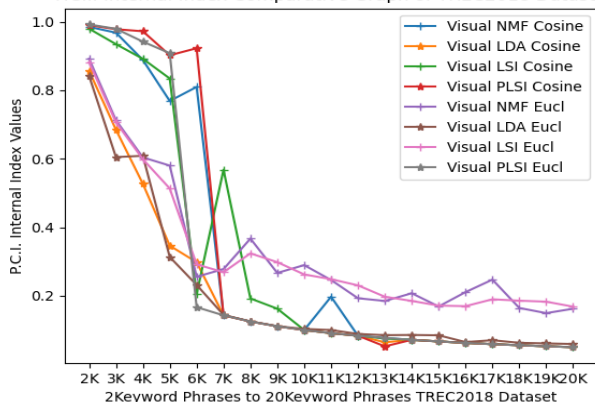
(f) Separation measure (SM) comparative results

X.I. Internal Index Comparative Graph of TREC2018 Dataset



(c) Xie-Beni index(XI) comparative results

P.C.I. Internal Index Comparative Graph of TREC2018 Dataset



(d) Partition coefficient Index (PCI) comparative results

Figure 4. TREC2018 internal validity indices

Figure 4(e) shows comparative performance values of partition coefficient internal index values, which range from 0 to $\log c$. In this case, its value range from 0 to 3 as indicated on the Y-axis line graph. The minimum value will be considered for higher performance in clustering. From this graph, infer that for 2 to 4 keywords, 6 keywords visual PLSI under Cosine, for 5 keywords, 7 keywords visual LSI under cosine, and 8 keywords, 10 keywords, 14 keywords, and 17 keywords visual NMF under Euclidean and rest of keywords visual LSI under Euclidean perform better.

Separation Measure internal index value is smaller then it will have greater performance. In this case, its value ranges from 0 to 10 as represented on the Y-axis. From this line graph, as shown in Figure 4(f), 2 keyword phrases to 5 keyword phrases visual LDA under Euclidean perform better and for the rest of keyword phrases, visual PLSI under cosine metric perform better than other models and also compared to Euclidean distance.

In Figure 5(a) to 5(d) external validity indices comparative results are shown. All external validity index value lies between 0 and 1. If values are nearer to 1, it indicates useful clustering, and appropriated keywords are placed in the appropriate cluster. From these bar graphs, interpret in all external validity indices visual NMF, visual LSI, and visual LDA under cosine metrics perform well, and their values are near to 1.

Figure 6(a) shows the comparative performance values of Davis-Bouldin (DB) internal index values under the coined and Euclidean metrics of TREC2015 keyword phrases. Its values range from 0 to 15 shown on the Y-axis. In the case of this index, the minimum value will perform better clustering results. From this graph on observation, inferred that visual NMF under cosine metric performs well when compared to the Euclidean metric for all models. Silhouette internal index (SI) values range from -1 to +1. If this index value is nearer to +1 then cluster performance will be best. If values decrease from +1 to -1 its performance also decreases. From the line graph as shown in Figure 6(b) Visual NMF under cosine metric performs well in all TREC2015 keyword phrases than that of Euclidean distance metric.

In Figure 6(c) Xie-Beni index (XI) internal validity index values under cosine and Euclidean metric are represented. Its

values range from 0 to 300 as represented on the Y-axis. The minimum value of this index will be considered as the best performance. This line-graph results were interpreted for 2keyword phrases and 3keyword phrases visual NMF performs well, whereas for 4keyword phrases and 5keyword phrases of TREC2015 visual LDA performs well. In all cases performs is better under cosine based validity index than Euclidean metric based. Partition coefficient index (PCI) values lie between 0 and 1. Maximum values will be considered as better performance, values nearer to 1 will be treated as best. From Figure 6(d), based on PCI comparative result values under Cosine and Euclidean metrics, Visual NMF, and Visual LSI both methods values are more significant than that of other values under Cosine metric based validity indices.

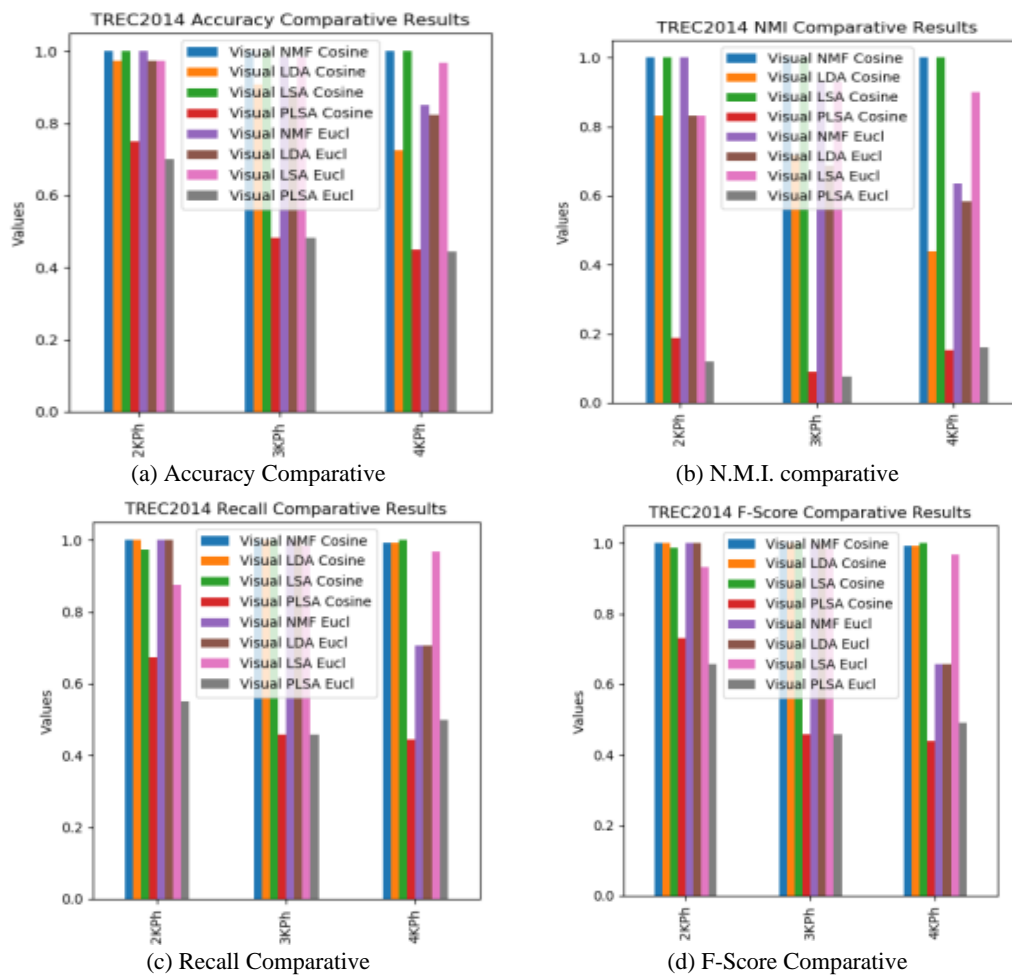
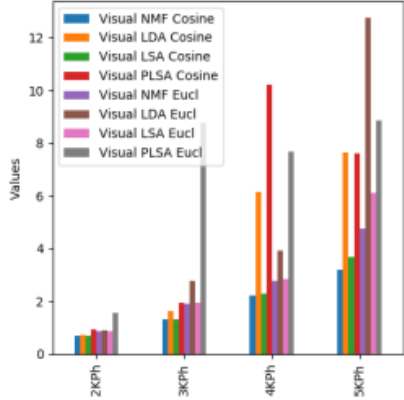


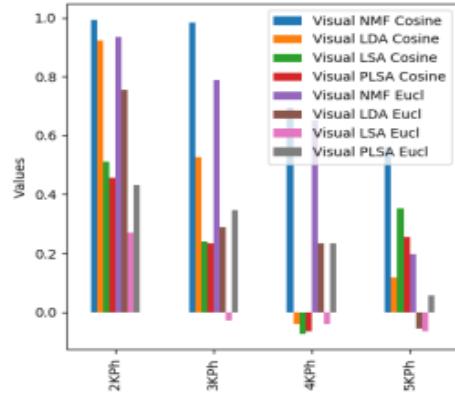
Figure 5. TREC2014 external validity indices comparative results

TREC2015 Davis-Bouldin(D.B.) Index Comparative Results



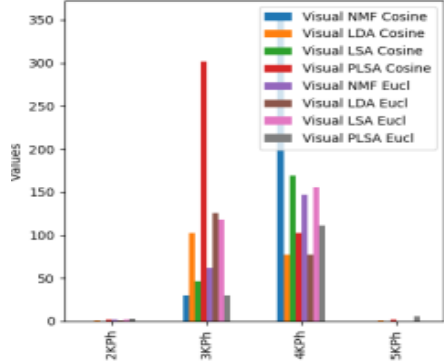
(a) Davies-Bouldin Index (DB)

TREC2015 Silhouette Index(S.I.) Comparative Results



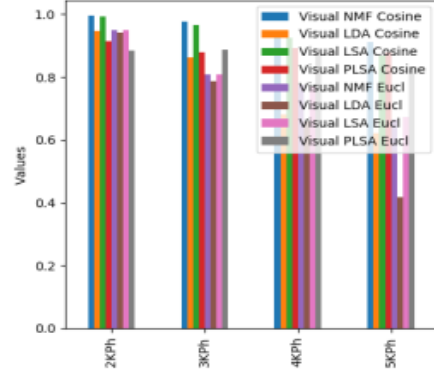
(b) Silhouette Index (SI)

TREC2015 Xie-ben Index(X.I.) Comparative Results



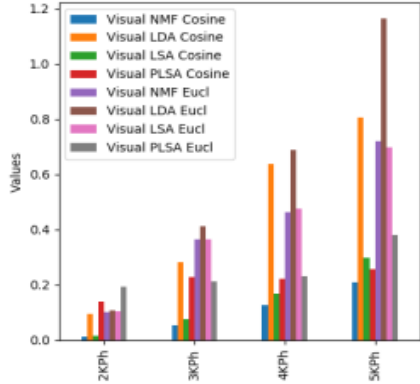
(c) Xie-Beni Index (XI)

TREC2015 Partition Coefficient Index(P.C.I.) Comparative



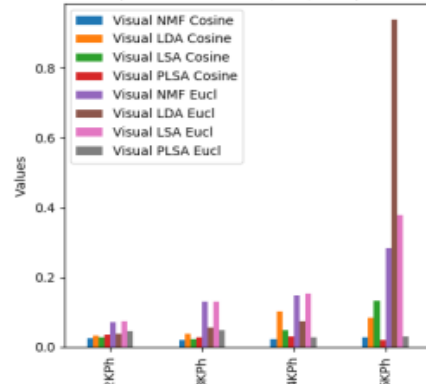
(d) Partition Coefficient (PCI)

TREC2015 Partition Entropy Index(P.E.I.) Comparative Resu



(e) PartitionEntropyIndex (PEI)

TREC2015 Separation Measure(S.M.) Comparative Result



(f) Separation Measure (SM)

Figure 6. TREC2015 Internal validity indices comparative results

Figure 6(e) shows comparative performance values of partition coefficient internal index values, ranging from 0 to $\log c$. Its value ranges from 0 to 1.2 as the number of keywords considered is only four, indicated on the Y-axis line graph. The minimum value will be considered for higher performance in clustering. From this graph, visual NMF values under cosine metric are more significant than that of Euclidean distance-based metrics. Separation Measure internal index value is smaller then it will have more remarkable performance.

In this case, its value ranges from 0 to 1 as represented on the Y-axis. This line graph shows in Figure 6(f), for 2keyword phrases and 3keyword phrases visual NMF, in case of 4keyword phrases, and 5 keyword phrases visual LDA. Both methods have better values under Cosine based metric validity index values than that of Euclidean based metric validity index values.

4.3 Cluster classification metrics to check elements in the cluster

4.3.1 External validity indices under cosine metric based on cluster classification metrics

In sections 4.2 and 4.3, cluster validity indices are calculated based on the confusion matrix and the number of clusters. Previous studies also cluster validation done using confusion matrices but not considered the elements in the cluster are well classified. In this paper, cluster validation is done by considering both confusion matrices and classification metrics to see that elements in the cluster are well classified or not. Cluster classification metrics are tabulated for all datasets for all four models under Cosine based and Euclidean metrics. Some sample results are represented from Table 4 to Table 9 for different datasets. In Table 4, external validity indices Precision (P), Recall (R), F-Score (F), Accuracy, Macro Average (M.A.), and Weighted

Average (W.A.) of 7 Topics Twitter datasets based on Cluster Classification under Cosine metric is presented. Here, seven topics are treated as seven clusters, and external validity indices results for each cluster are represented by considering every document in that particular cluster where Support (SU) represents the number of documents present in that cluster.

Table 5, external validity indices of 10 Topics Twitter datasets for Visual NMF and Visual LDA hybrid topic models based on Cluster Classification metrics under Cosine metric, is tabulated. Here, ten topics are treated as ten clusters, and external validity indices results for each cluster are represented by considering every document in that particular cluster where

Support (SU) represents the number of documents present in that cluster.

4.3.2 Comparative results of external validity indices based on cluster classification

In this paper, a comparative study of external validity indices based on cluster classifications metrics also performed for different hybrid topic models under Cosine based and Euclidean based metrics. Experimental results are tabulated for all types of datasets mentioned in the datasets description section. Sample of comparative results of external validity indices based on cluster classification for 20 keyword phrases of TREC2018 datasets is mentioned in Table 6 to Table 9.

Table 4. External validity indices based on cluster classification of 7 topics Twitter datasets

Visual LSI under Cosine metric					Visual PLSI under Cosine metric						
Cl#	P	R	F	SU	Cl#	P	R	F	SU		
1	0.550	0.550	0.550	40	1	0.250	0.250	0.250	40		
2	0.350	0.350	0.350	40	2	0.300	0.300	0.300	40		
3	0.625	0.625	0.625	40	3	0.325	0.325	0.325	40		
4	0.525	0.525	0.525	40	4	0.275	0.275	0.275	40		
5	0.675	0.675	0.675	40	5	0.225	0.225	0.225	40		
6	0.700	0.700	0.700	40	6	0.200	0.200	0.200	40		
7	0.200	0.200	0.200	40	7	0.225	0.225	0.225	40		
Accuracy				0.518	280	Accuracy				0.257	280
M.A				0.518	280	M.A				0.257	280
W.A				0.518	280	W.A				0.257	280

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

Table 5. External validity indices based on cluster classification metrics of 10 topics Twitter datasets

Visual NMF under Cosine metric					Visual LDA under Cosine metric						
Cl#	P	R	F	SU	Cl#	P	R	F	SU		
1	0.800	0.800	0.800	50	1	0.240	0.240	0.240	50		
2	0.400	0.600	0.480	20	2	0.200	0.150	0.171	20		
3	0.714	0.385	0.500	65	3	0.246	0.246	0.246	65		
4	0.457	0.457	0.457	35	4	0.157	0.314	0.210	35		
5	0.822	0.529	0.643	70	5	0.257	0.129	0.171	70		
6	0.550	0.244	0.338	45	6	0.229	0.178	0.200	45		
7	0.323	0.700	0.442	30	7	0.133	0.133	0.133	30		
8	0.543	0.543	0.543	35	8	0.111	0.143	0.125	35		
9	0.247	0.514	0.343	35	9	0.229	0.229	0.229	35		
10	0.000	0.000	0.000	15	10	0.100	0.133	0.114	15		
Accuracy				0.497	400	Accuracy				0.195	280
M.A				0.487	400	M.A				0.190	400
W.A				0.576	400	W.A				0.208	400

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

Table 6. Comparative results of validity indices (Visual NMF) based on Cluster Classification for 20 Keyword Phrases of TREC2018 Datasets

Visual NMF under Cosine metric					Visual NMF under Eucl metric				
Cl#	P	R	F	SU	Cl#	P	R	F	SU
1	0.740	0.740	0.740	50	1	0.740	0.740	0.740	50
2	0.300	0.375	0.333	40	2	0.300	0.375	0.333	40
3	0.306	0.578	0.400	45	3	0.306	0.578	0.400	45
4	0.200	0.200	0.200	35	4	0.200	0.200	0.200	35
5	0.440	0.367	0.400	30	5	0.440	0.367	0.400	30
6	0.543	0.224	0.317	85	6	0.543	0.224	0.317	85
7	0.733	0.440	0.550	50	7	0.733	0.440	0.550	50
8	0.880	0.400	0.550	55	8	0.880	0.400	0.550	55
9	0.289	0.371	0.325	35	9	0.289	0.371	0.325	35
10	0.000	0.000	0.000	15	10	0.000	0.000	0.000	15
11	0.000	0.000	0.000	30	11	0.000	0.000	0.000	30
12	0.325	0.650	0.433	20	12	0.325	0.650	0.433	20
13	0.129	0.360	0.189	25	13	0.129	0.360	0.189	25
14	0.600	0.514	0.554	35	14	0.600	0.514	0.554	35

15	0.400	0.286	0.333	70	15	0.400	0.286	0.333	70
16	0.771	0.600	0.675	45	16	0.771	0.600	0.675	45
17	0.436	0.480	0.453	50	17	0.436	0.480	0.453	50
18	0.086	0.086	0.086	35	18	0.086	0.086	0.086	35
19	0.511	0.920	0.657	25	19	0.511	0.920	0.657	25
20	0.067	0.040	0.050	25	20	0.067	0.040	0.050	25
Accuracy			0.388	800	Accuracy			0.388	800
M.A	0.388	0.382	0.362	800	M.A	0.388	0.382	0.362	800
W.A	0.446	0.388	0.392	800	W.A	0.446	0.388	0.392	800

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

Table 7. Comparative results of validity indices (Visual LDA) based on Cluster Classification for 20 Keyword Phrases of TREC2018 Datasets

Visual LDA under Cosine metric					Visual LDA under Eucl metric				
Cl#	P	R	F	SU	Cl#	P	R	F	SU
1	0.171	0.120	0.141	50	1	0.160	0.160	0.160	50
2	0.109	0.150	0.126	40	2	0.167	0.125	0.143	40
3	0.100	0.111	0.105	45	3	0.171	0.133	0.150	45
4	0.160	0.144	0.133	35	4	0.100	0.200	0.133	35
5	0.086	0.100	0.092	30	5	0.150	0.100	0.120	30
6	0.167	0.100	0.125	85	6	0.212	0.212	0.212	85
7	0.167	0.100	0.125	50	7	0.160	0.080	0.107	50
8	0.171	0.218	0.192	55	8	0.171	0.109	0.133	55
9	0.100	0.086	0.092	35	9	0.156	0.200	0.175	35
10	0.120	0.200	0.150	15	10	0.080	0.133	0.100	15
11	0.100	0.067	0.080	30	11	0.133	0.067	0.089	30
12	0.067	0.050	0.057	20	12	0.080	0.200	0.114	20
13	0.114	0.160	0.133	25	13	0.109	0.240	0.150	25
14	0.111	0.143	0.125	35	14	0.222	0.286	0.250	35
15	0.150	0.086	0.109	70	15	0.286	0.143	0.190	70
16	0.143	0.111	0.125	45	16	0.143	0.111	0.125	45
17	0.244	0.220	0.232	50	17	0.200	0.100	0.133	50
18	0.220	0.314	0.259	35	18	1.100	0.143	0.118	35
19	0.120	0.120	0.120	25	19	0.100	0.160	0.123	25
20	0.100	0.200	0.133	25	20	0.067	0.080	0.073	25
Accuracy			0.142	800	Accuracy			0.149	800
M.A	0.136	0.142	0.135	800	M.A	0.148	0.149	0.140	800
W.A	0.145	0.142	0.140	800	W.A	0.166	0.149	0.149	800

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

Comparative results of validity indices of 20 keyword phrases of TREC2018 for Visual NMF hybrid topic model is mentioned in Table 6. From these results inferred that both results are the same under two distance metrics for all twenty clusters.

In Table 7, comparative results of validity indices are shown under cosine and Euclidean based metrics for the Visual LDA model. From these results, interpreted Euclidean based metric on average for all clusters perform better than cosine based metric.

Table 8. Comparative results of validity indices (Visual LSI) based on Cluster Classification for 20 Keyword Phrases of TREC2018 Datasets

Visual LSI under Cosine metric					Visual LSI under Euclidean metric				
Cl#	P	R	F	SU	Cl#	P	R	F	SU
1	0.200	0.140	0.165	50	1	0.840	0.420	0.560	50
2	0.200	0.150	0.171	40	2	0.340	0.425	0.378	40
3	0.380	0.422	0.400	45	3	0.375	0.333	0.353	45
4	0.200	0.143	0.167	35	4	0.600	0.429	0.500	35
5	0.300	0.300	0.300	30	5	0.100	0.067	0.080	30
6	0.660	0.388	0.489	85	6	0.486	0.200	0.283	85
7	0.240	0.120	0.160	50	7	0.133	0.080	0.100	50
8	0.514	0.327	0.400	55	8	0.422	0.345	0.080	55
9	0.200	0.229	0.213	35	9	0.540	0.771	0.635	35
10	0.222	0.667	0.333	15	10	0.000	0.000	0.000	15
11	0.000	0.000	0.000	30	11	0.171	0.200	0.185	30
12	0.200	0.350	0.255	20	12	0.267	0.600	0.369	20
13	0.086	0.240	0.126	25	13	0.133	0.080	0.100	25
14	0.080	0.057	0.067	35	14	0.388	0.943	0.550	35
15	0.235	0.286	0.258	70	15	0.329	0.329	0.329	70

16	0.400	0.489	0.440	45	16	0.333	0.222	0.267	45		
17	0.089	0.080	0.084	50	17	0.686	0.480	0.565	50		
18	0.114	0.114	0.114	35	18	0.540	0.771	0.635	35		
19	0.150	0.120	0.133	25	19	0.171	0.240	0.200	25		
20	0.200	0.400	0.267	25	20	0.364	0.800	0.500	25		
Accuracy				0.249	800	Accuracy				0.375	800
M.A	0.234	0.251	0.227	800	M.A	0.361	0.387	0.348	800		
W.A	0.273	0.249	0.248	800	W.A	0.398	0.375	0.361	800		

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

Table 9. Comparative results of validity indices (Visual PLSI) based on cluster classification for 20 keyword phrases of TREC2018 datasets

Visual PLSI under Cosine metric					Visual PLSI under Euclidean metric						
Cl #	P	R	F	SU	Cl #	P	R	F	SU		
1	0.200	0.180	0.189	50	1	0.200	0.200	0.200	50		
2	0.140	0.175	0.156	40	2	0.080	0.050	0.062	40		
3	0.111	0.111	0.111	45	3	0.267	0.267	0.267	45		
4	0.160	0.229	0.188	35	4	0.067	0.086	0.075	35		
5	0.100	0.233	0.140	30	5	0.114	0.133	0.123	30		
6	0.300	0.106	0.157	85	6	0.176	0.176	0.176	85		
7	0.114	0.080	0.094	50	7	0.167	0.100	0.125	50		
8	0.164	0.164	0.164	55	8	0.200	0.127	0.156	55		
9	0.100	0.057	0.073	35	9	0.100	0.057	0.073	35		
10	0.100	0.267	0.145	15	10	0.060	0.200	0.092	15		
11	0.114	0.133	0.123	30	11	0.160	0.133	0.145	30		
12	0.029	0.050	0.036	20	12	0.133	0.100	0.144	20		
13	0.120	0.120	0.120	25	13	0.100	0.160	0.123	25		
14	0.160	0.114	0.133	35	14	0.114	0.114	0.114	35		
15	0.165	0.200	0.181	70	15	0.200	0.200	0.200	70		
16	0.133	0.089	0.107	45	16	0.127	0.156	0.140	45		
17	0.171	0.120	0.141	50	17	0.171	0.120	0.141	50		
18	0.140	0.200	0.165	35	18	0.133	0.114	0.123	35		
19	0.120	0.120	0.120	25	19	0.160	0.160	0.160	25		
20	0.200	0.120	0.150	25	20	0.080	0.160	0.107	25		
Accuracy				0.141	800	Accuracy				0.145	800
M.A	0.142	0.143	0.135	800	M.A	0.141	0.141	0.136	800		
W.A	0.158	0.141	0.140	800	W.A	0.153	0.145	0.146	800		

CL#: Cluster Number; P: Precision; R: Recall; F: F-Score; SU: Support; M.A.: Macro Average; W.A.: Weighted Average

The quantitative validity indices of 20 keyword phrases of TREC2018 for the Visual LSI hybrid topic model are mentioned in Table 8. From these results, Euclidean results are better than that of cosine based on accuracy, Macro Average, and Weighted Average.

In Table 9, comparative results of validity indices based on cluster classification metrics are shown under Cosine and Euclidean based metrics. These results interpreted that Euclidean based metric on average for all clusters to perform better than cosine based metric.

5. CONCLUSION AND FUTURE SCOPE

The cosine-based validation metrics proposed in this paper have the advantage of considering both in the implementation of hybrid topic models clustering algorithms and the validation of formed clusters. Nearness among documents in terms of topics is also quantified by the closeness between two different documents and their lexical similarity. In this point of view, proposed cosine-based metrics are more desirable than Euclidean metrics, where merely the distance between two clusters will be considered in document clustering. This paper in cluster validation compactness, separation, number of clusters, and classification metrics is considered, which will evaluate the classification by considering every element in all

clusters of a corpus. Experimentally proved proposed novel cosine based internal and external validity indices work well in cluster validation and improve the effectiveness of cluster than that of Euclidean validity metrics. However, in high sparsity, other aspects such as density should also be considered in the evaluation. Performance can be optimized by increasing the scalability of their execution in a semi-distributed environment and dealing with dynamically changing large datasets in text documents clustering applications.

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